

Incorporating Decision-Maker's Preferences into the Automatic Configuration of Bi-objective Optimisation Algorithms

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The Joint Lectures on Evolutionary Algorithms (JoLEA)

15 February 2023



The University of Manchester
Alliance Manchester Business School



Who am I?

- Senior Lecturer (Assoc. Prof.) at AMBS (UoM), 2015–



The University of Manchester
Alliance Manchester Business School

- Senior Distinguished Researcher, University of Málaga, 2020–2022



UNIVERSIDAD
DE MÁLAGA

- Editor-in-Chief of GECCO 2019



- Committee Chair of the ACM SIGEVO Dissertation Award

- (co-)Editor-in-Chief of
ACM Transactions on Evolutionary Learning and Optimization (TELO)



My research is about ...

- Benchmarking and Empirical Analysis of Optimization Algorithms
 - 👉 Reproducibility in Evolutionary Computation [López-Ibáñez, Branke & Paquete, 2021]
- Multi-objective optimization 👉 EAF package
- Interactive optimization (human-in-the-loop)
 - 👉 Machine Decision Makers [López-Ibáñez & Knowles, 2015]
- Automatic configuration, selection and design of algorithms 👉 irace
- Expensive optimization ...
- Applications, applications, applications!
 - School bus routing for SEND students
 - Optimization in steel manufacturing
 - Supply chain design for Personalised Medicine
 - Bayesian Optimisation with dynamic constraints
 - Patient scheduling



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Today's topic



Juan E. Diaz Leiva



Manuel López-Ibáñez



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Juan Esteban Diaz and Manuel López-Ibáñez,

Incorporating decision-maker's preferences into the automatic configuration of bi-objective optimisation algorithms,

European Journal of Operational Research, 289:3, 16 March 2021, pages 1209–1222.

<https://doi.org/10.1016/j.ejor.2020.07.059>

★ EJOR Editors' Choice Article, January 2021

Agenda

- (1) Automatic algorithm configuration
- (2) Bi-objective optimization
- (3) The empirical attainment function (EAF)
- (4) Incorporating decision-maker's preferences into the automatic configuration of bi-objective optimisation algorithms

Design choices and parameters everywhere

Modern high-performance optimizers involve a large number of design choices and (hyper)-parameter settings

- Exact solvers

- Design choices: alternative models, pre-processing, variable selection, value selection, branching rules ...
+ numerical parameters
- IBM CPLEX: 63 parameters that control the optimization

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 - IBM CPLEX: 63 parameters that control the optimization
- (Meta)-heuristic solvers
 - Design choices: solution representation, operators, neighborhoods, pre-processing, strategies, . . . + numerical parameters
 - Many are *hidden*

Design choices and parameters everywhere

Modern high-performance **optimizers** software involve a large number of design choices and (hyper)-parameter settings

Domain	Software	Parameters	
ML	WEKA	768	[Kotthoff et al., 2016]
	Auto-sklearn	110	[Feurer et al., 2015]
AI Planning	LGP,	45 – 66	[Vallati et al., 2011]
	Fast-downward		[Fawcett et al., 2011]
Code optimization	GCC	172 flags + 195 numerical	[Pérez Cáceres et al., 2017]

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Design choices and parameters everywhere

- *categorical* parameters

recombination $\in \{ \text{uniform, one-point, two-point} \}$

localsearch $\in \{ \text{tabu search, SA, ILS} \}$

- *ordinal* parameters

neighborhoods $\in \{ \text{small, medium, large} \}$

- *numerical* parameters

population sizes, acceptance temperature,
hidden constants, ...

- Parameters may be *conditional* to specific values of other parameters:

temperature only enabled if localsearch == "SA"

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*Configuring an algorithm involves setting
categorical, ordinal and numerical parameters*

The algorithm configuration problem

- ① Find the best algorithm configuration
given a set of *training problem instances*

- ② Repeatedly use this algorithm configuration to solve
unseen problem instances

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A problem with many names:

offline parameter *tuning*,
automatic algorithm configuration,
hyper-parameter optimization,
hyper-heuristics, genetic programming,
meta-optimisation, programming by optimisation [Hoos, 2012], ...

Automatic Algorithm Configuration: How?

A mixed-integer stochastic black-box optimization problem

- Mixed decision variables:
categorical, ordinal and numerical (real-valued and integer)
- Stochasticity from algorithm and problem instances
- Black-box: evaluation requires running the algorithm

Automatic Algorithm Configuration: How?

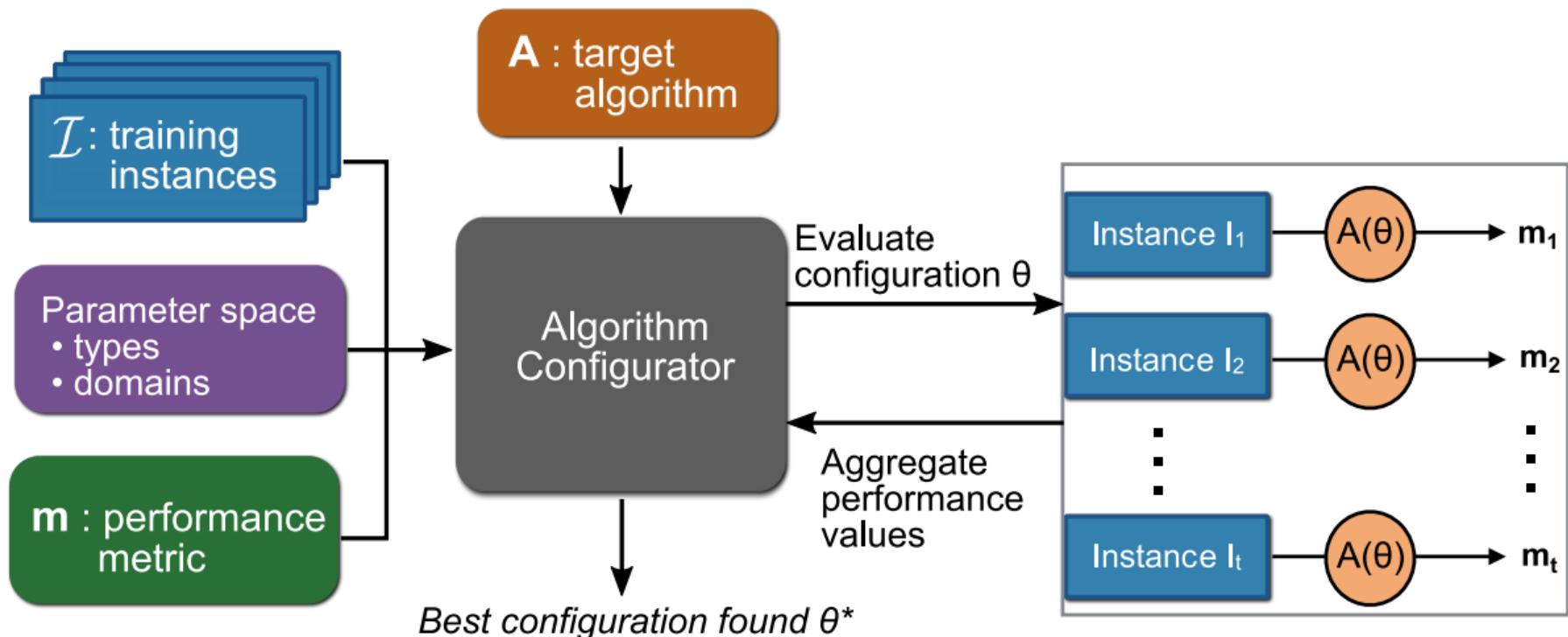
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Methods for Automatic Algorithm Configuration

- **SPOT** [Bartz-Beielstein, Lasarczyk & Preuss, 2005]
- **ParamILS** [Hutter, Hoos & Stützle, 2007]
- **SMAC** [Hutter, Hoos & Leyton-Brown, 2011]
- **IRACE** [López-Ibáñez, Dubois-Lacoste, Stützle & Birattari, 2011]
[López-Ibáñez, Dubois-Lacoste, Pérez Cáceres, Stützle & Birattari, 2016]

Automatic Algorithm Configuration



Bi-objective Optimisation

Two objective functions: $\vec{f} = (f_1(x), f_2(x))$

How to minimize both of them?

Bi-objective Optimisation

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How to minimize both of them?

- *A priori* knowledge / preferences known
 - ☞ Aggregate into a scalar value:

$$f_s(x) = \lambda \cdot f_1(x) + (1 - \lambda) \cdot f_2(x)$$

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Bi-objective Optimisation

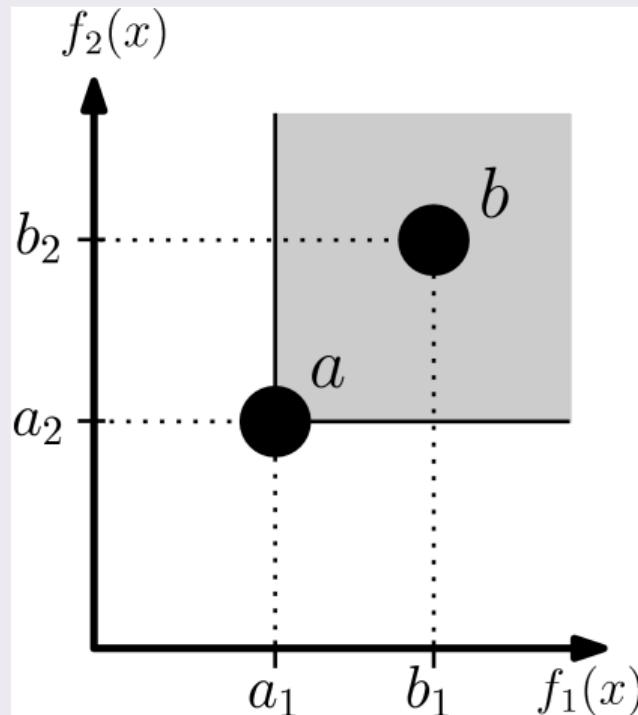
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a dominates b

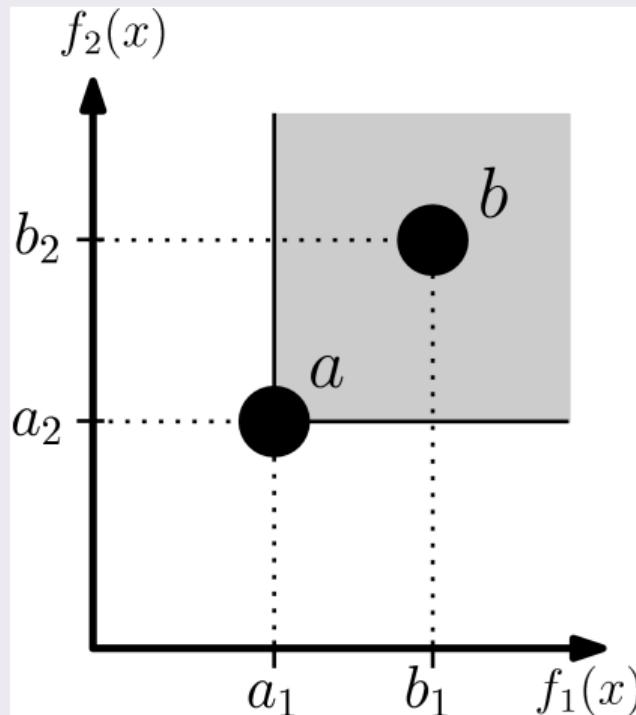


Bi-objective Optimisation

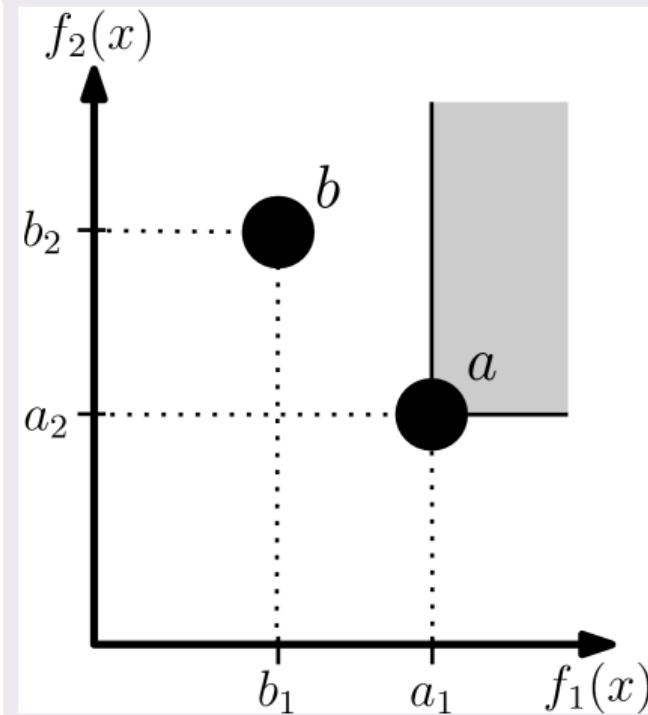
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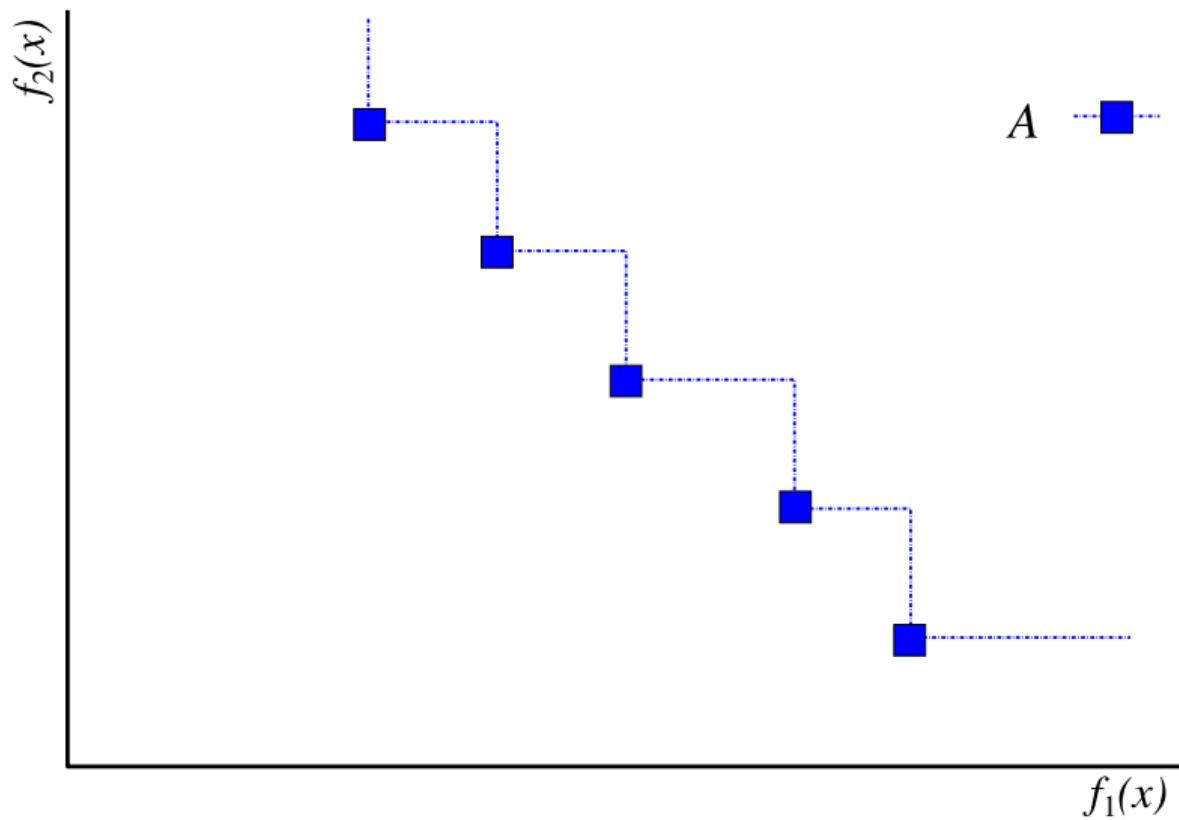
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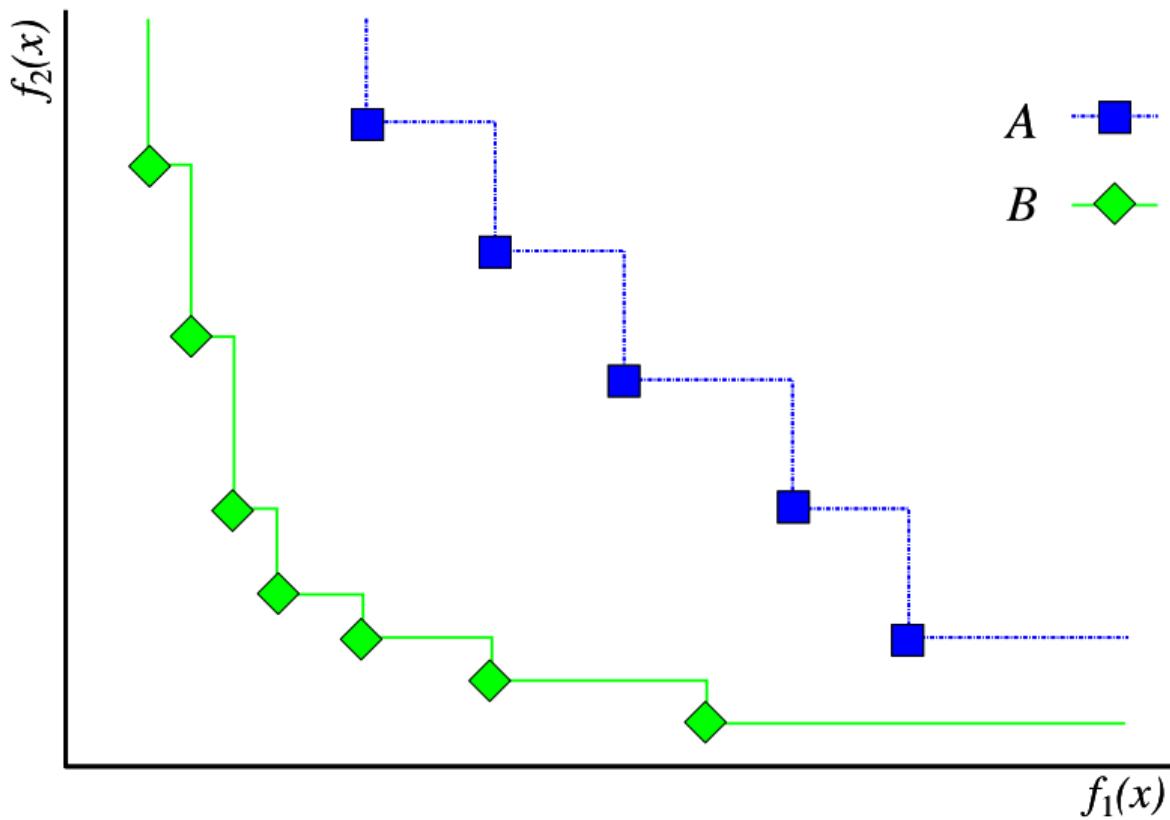
a and b nondominated



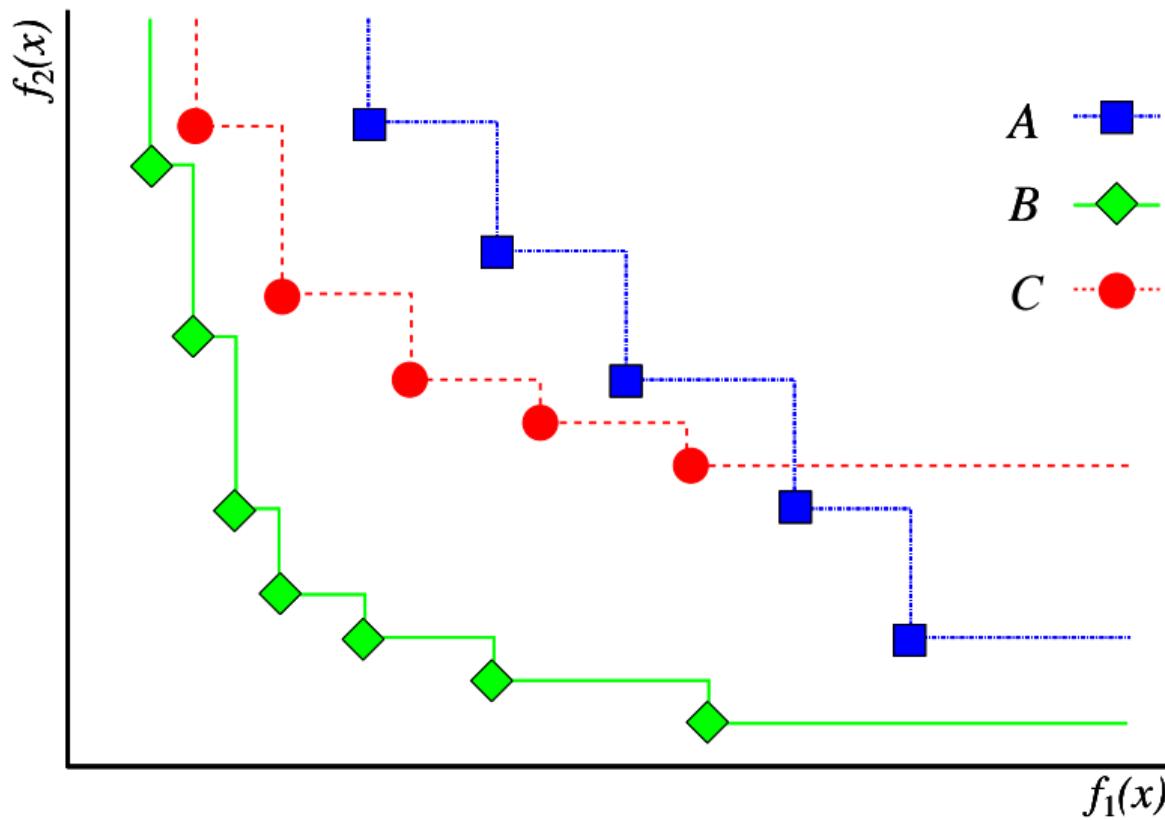
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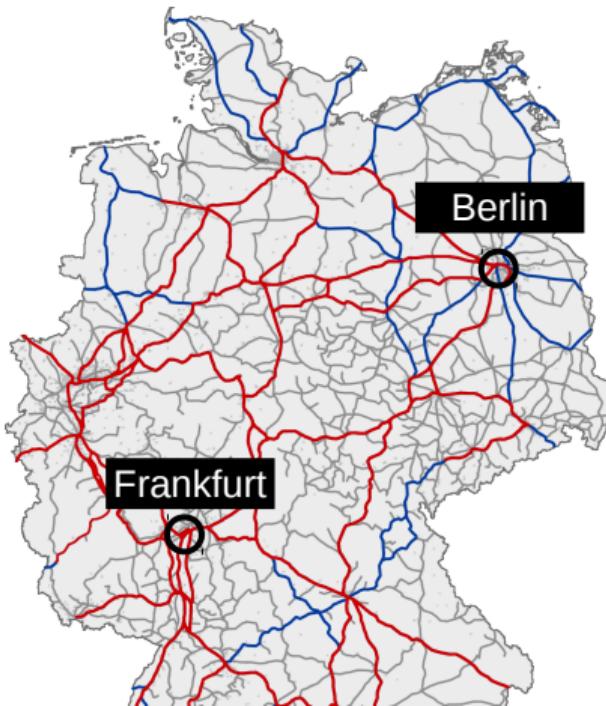


Stochastic Multi-criteria Data

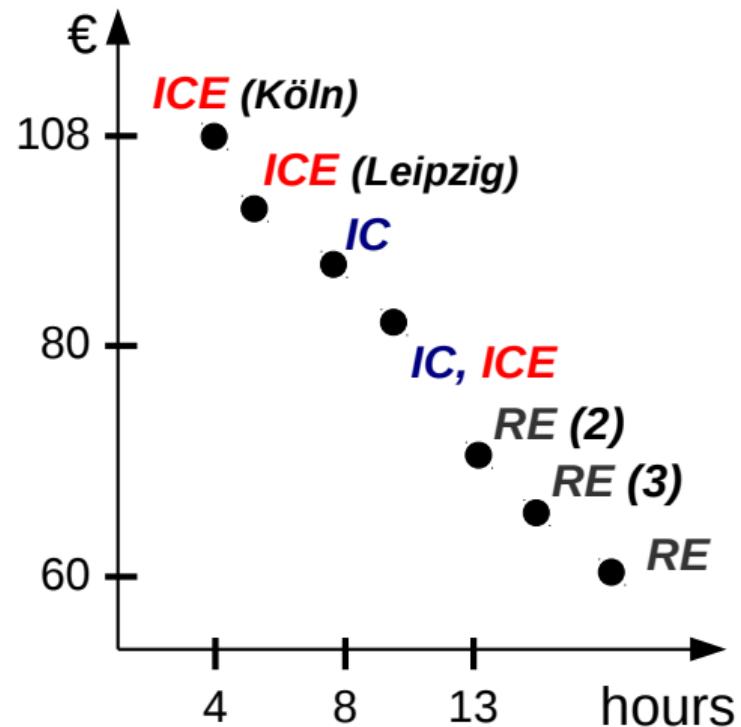
Expensive → Cheap

ICE EC, IC RE, RB

Fast → Slow



Fastest and cheapest train trip from Frankfurt to Berlin?

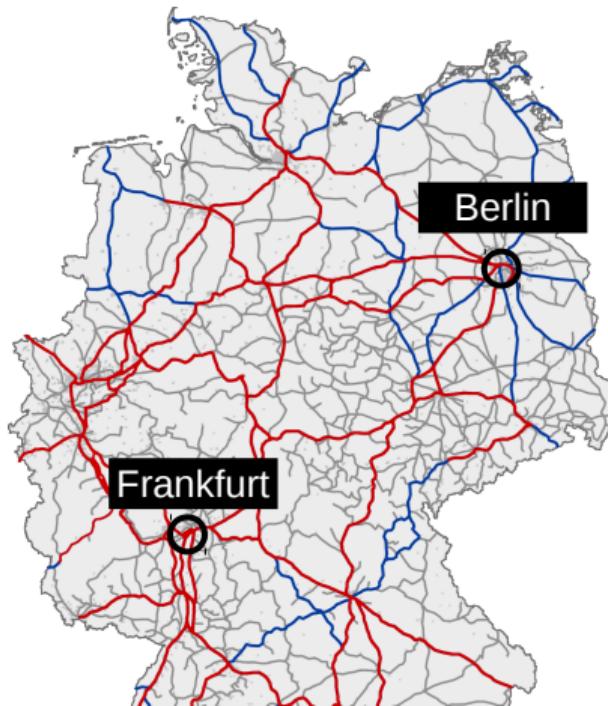


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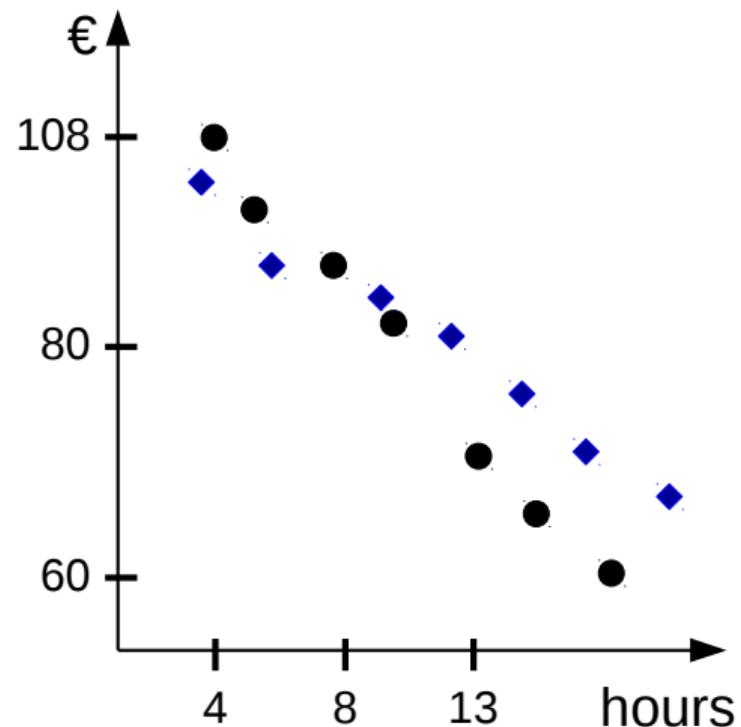
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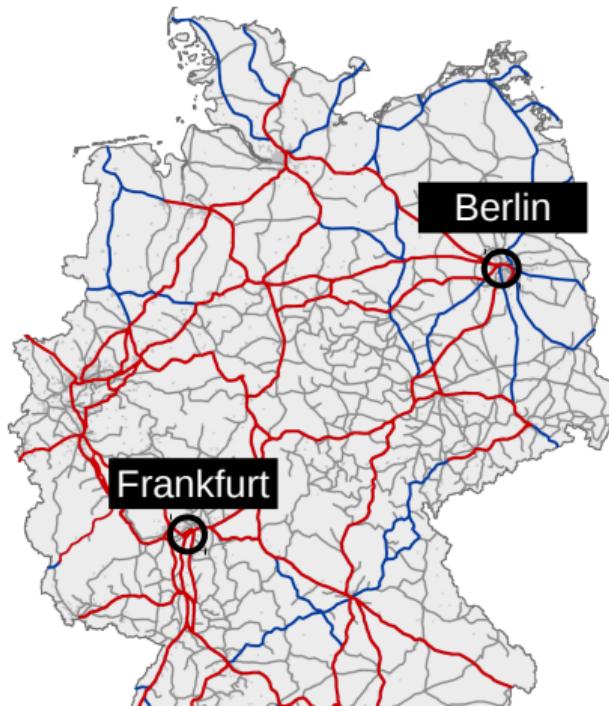


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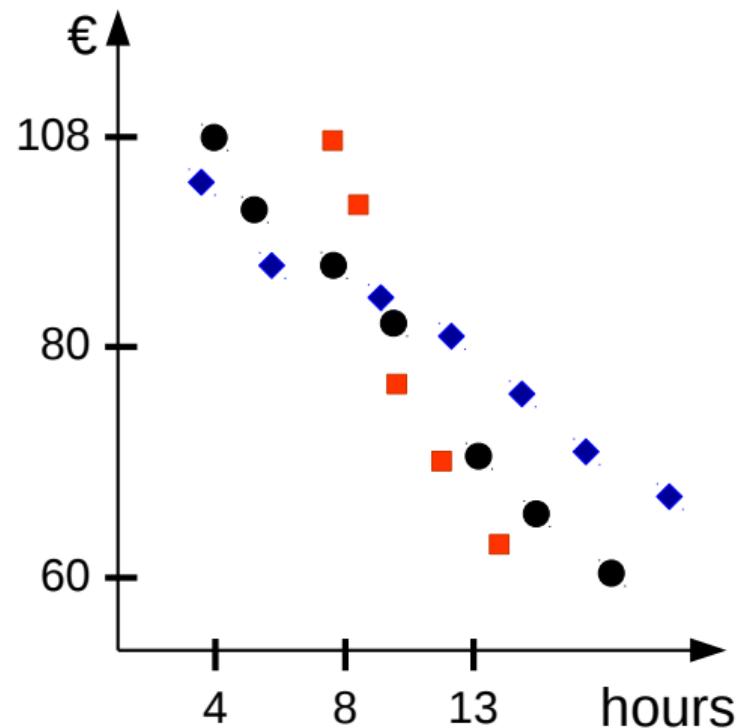
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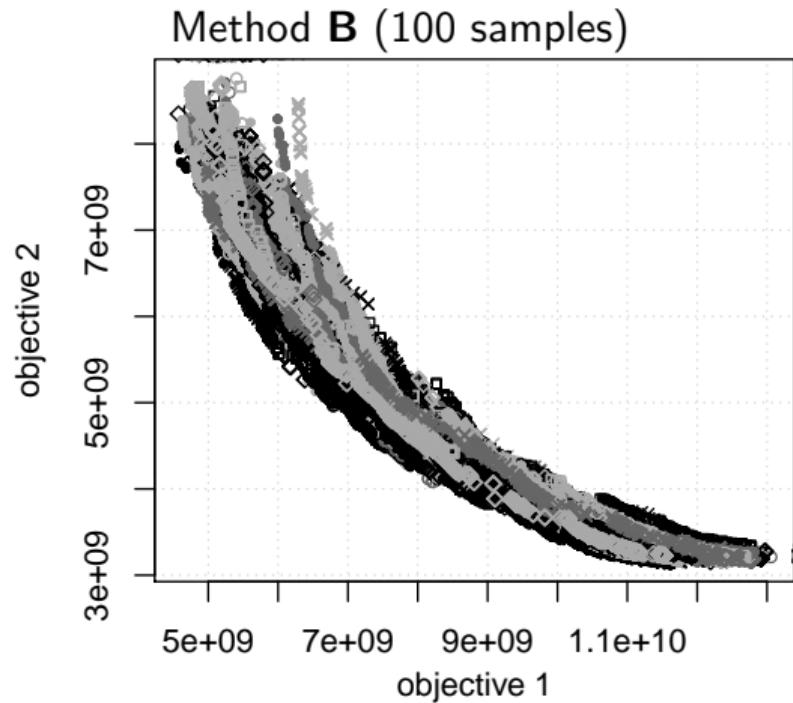
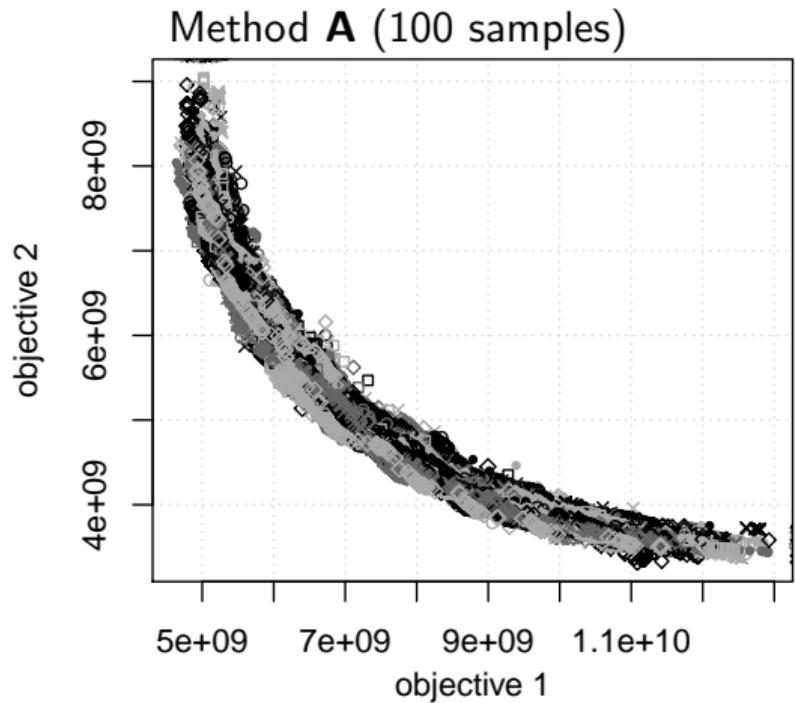
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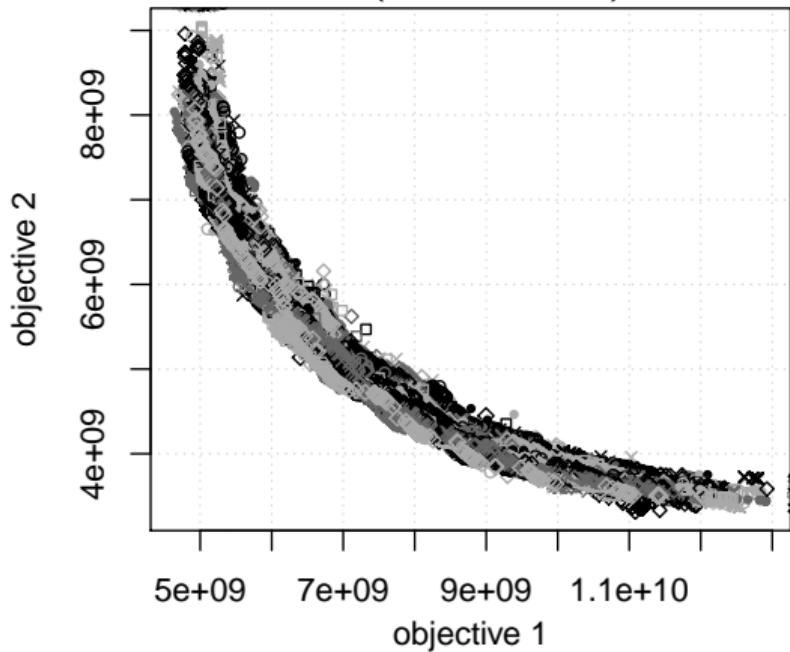


Stochastic Nondominated Sets

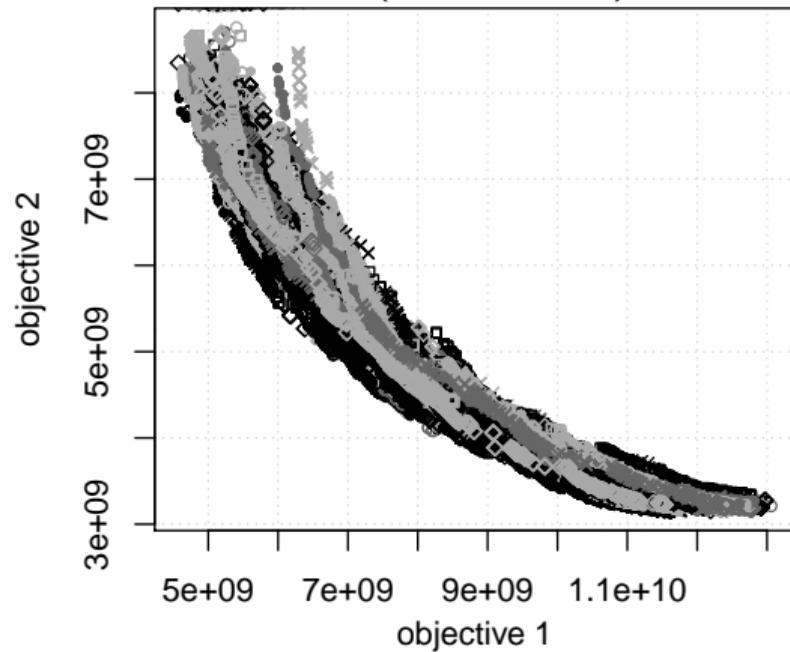


Stochastic Nondominated Sets

Method **A** (100 samples)



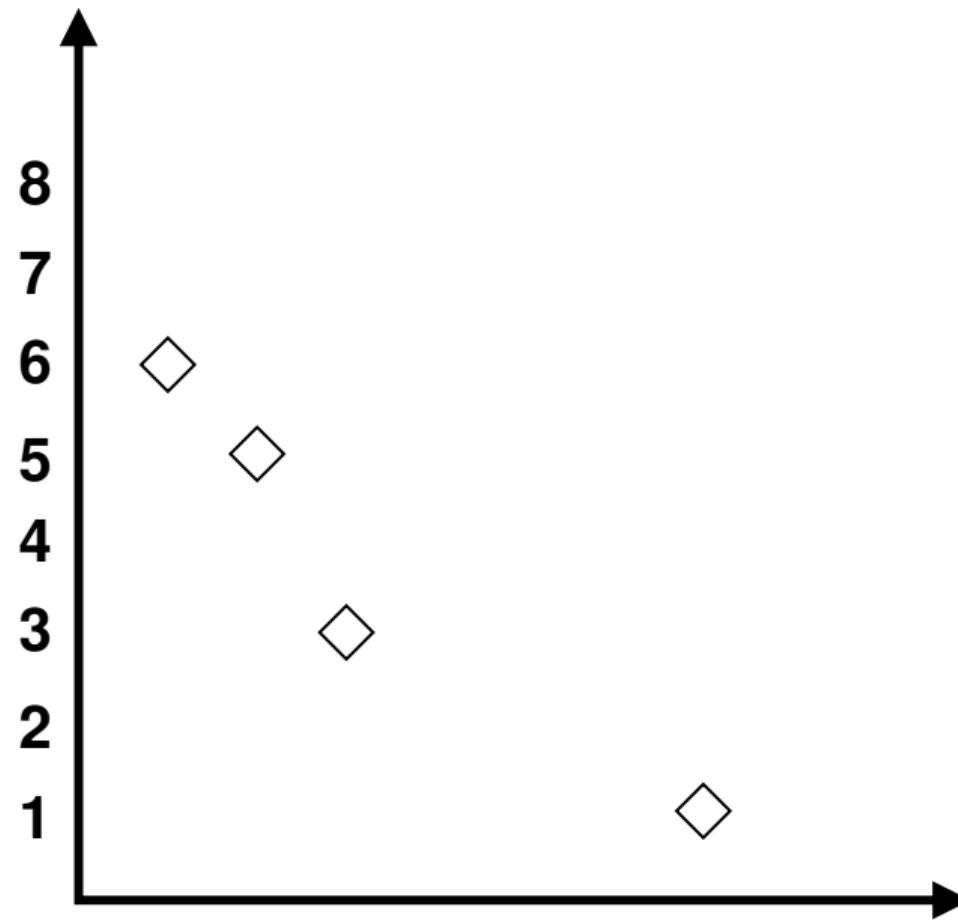
Method **B** (100 samples)



Which one is better?

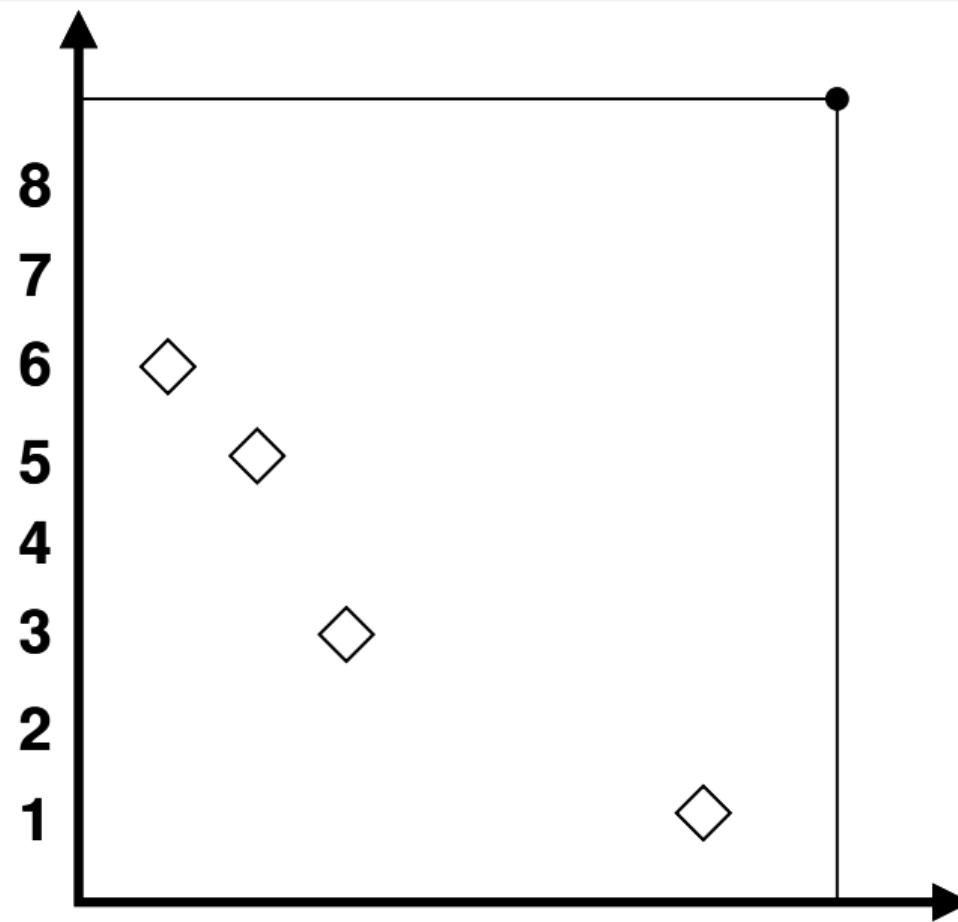
Hypervolume metric

[Knowles & Corne, 2003; Zitzler et al., 2003]



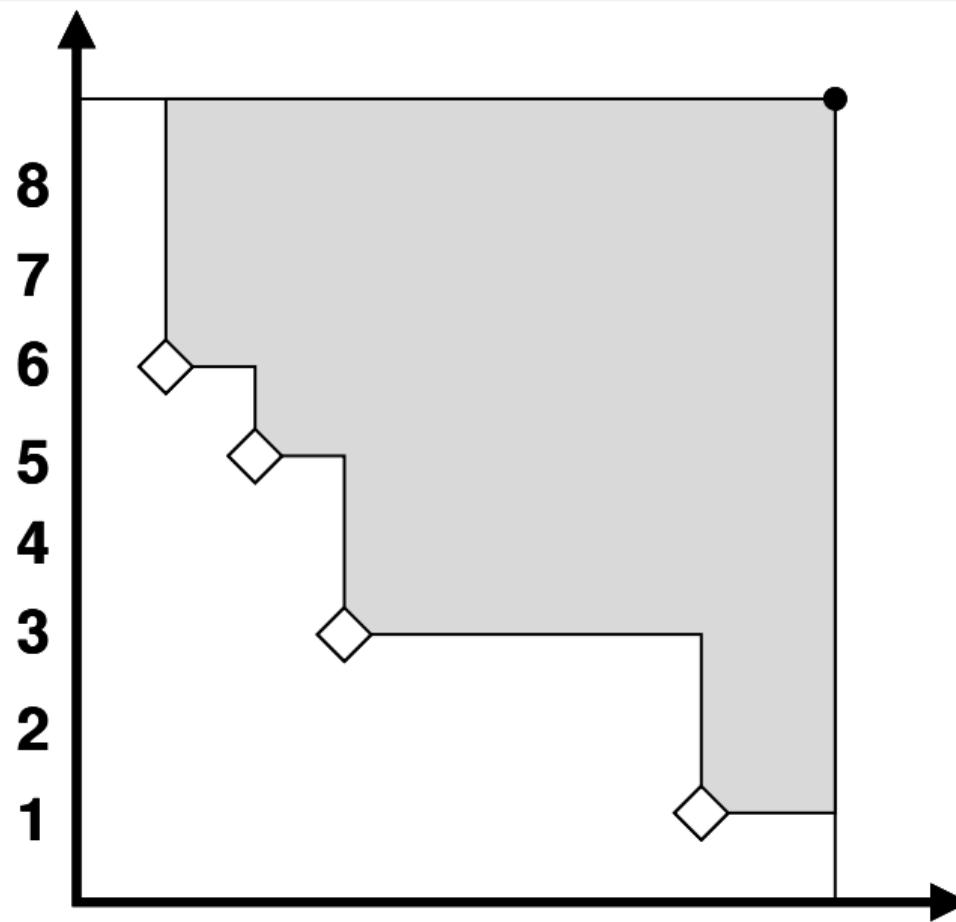
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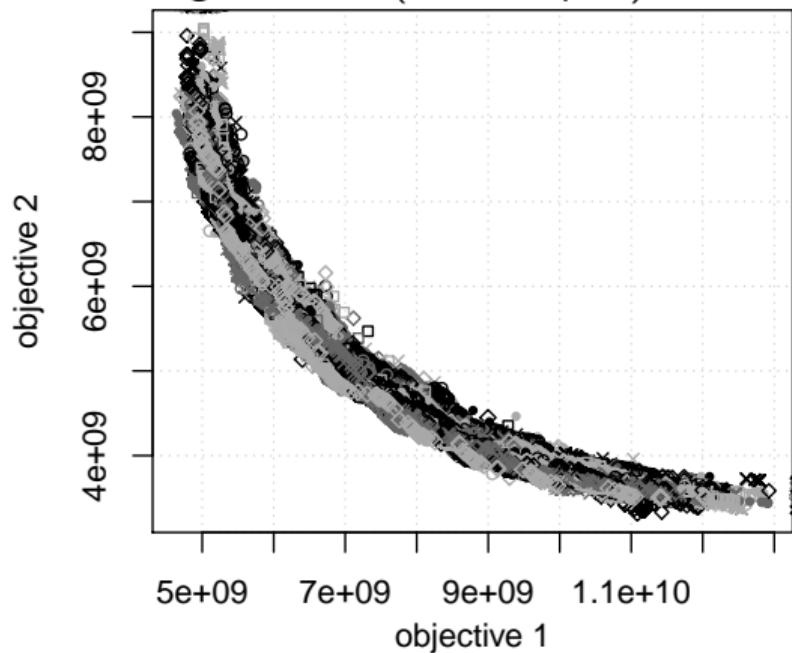
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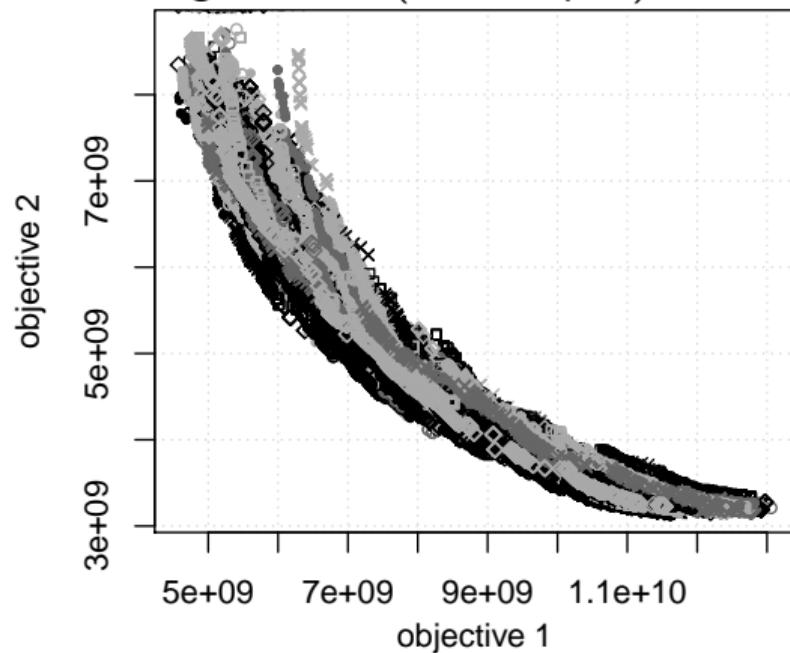
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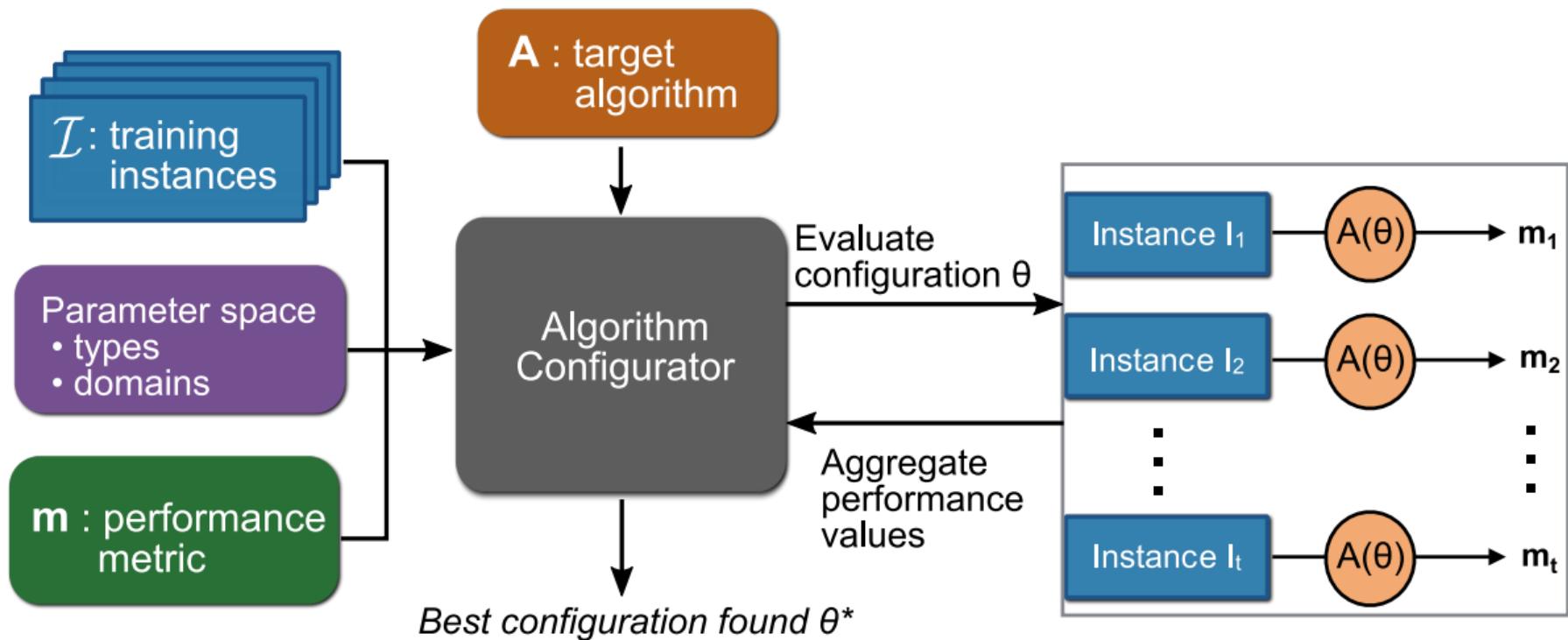
Mean HV = 0.920016

Algorithm **B** (100 samples)



Mean HV = 0.9070087

Automatic Configuration of Multi-Objective Optimizers



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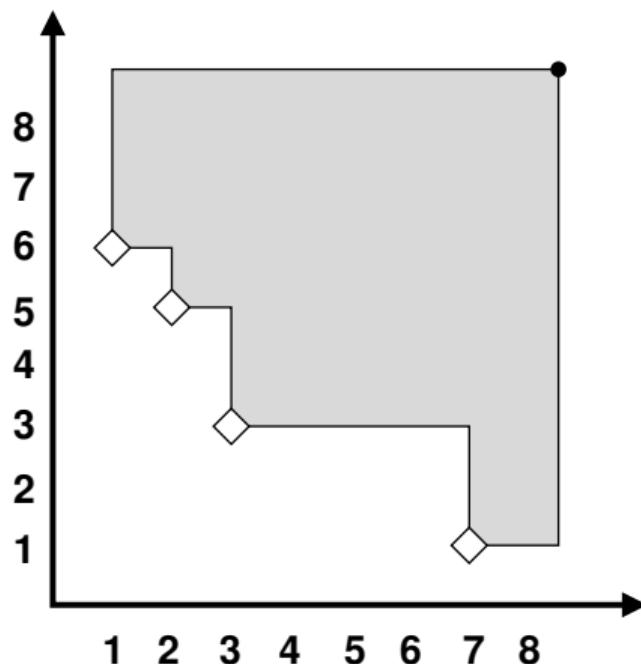
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 - Algorithm's output is an approximation to the PF
 - AC performance metric is scalar

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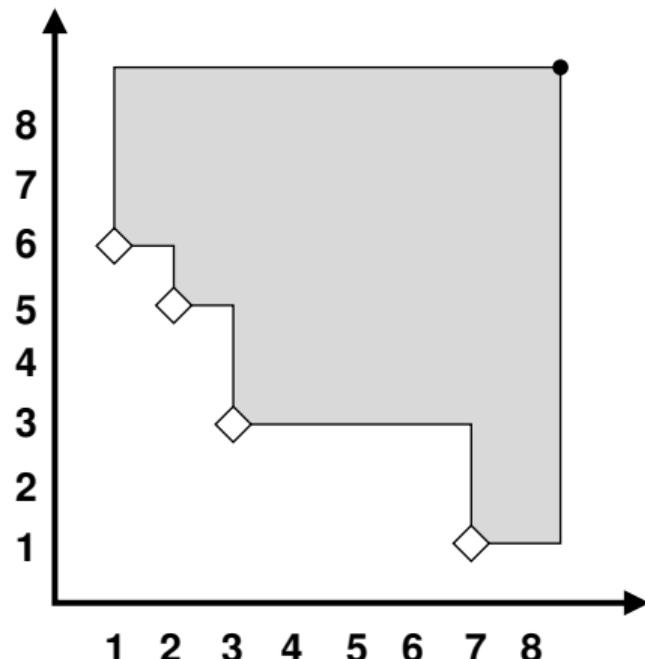
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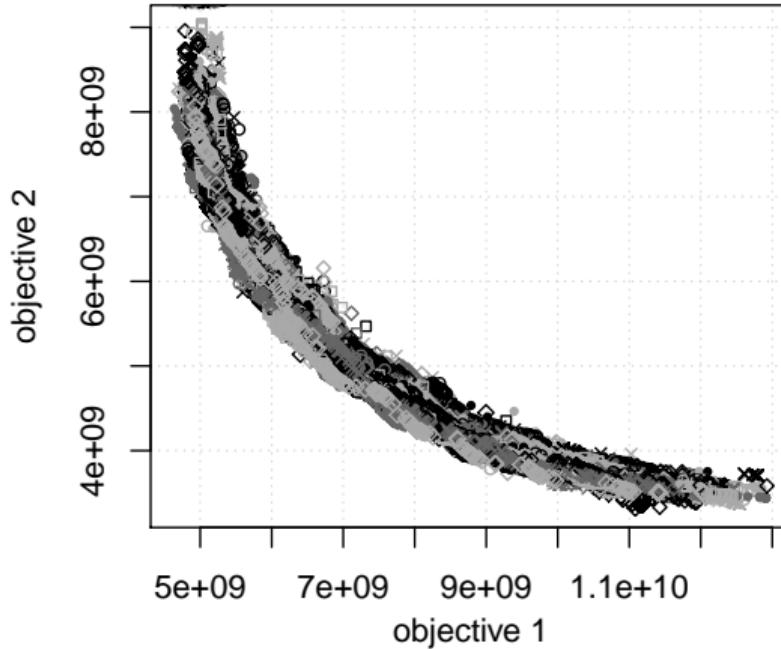
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- TP+PLS: Multi-objective local search framework for PFSP [Dubois-Lacoste et al., 2011]
- Multi/Many-objective Evolutionary Algorithms (AutoMOEA) [Bezerra et al., 2016, 2020a]
- Anytime behavior of exact and heuristic algorithms [López-Ibáñez & Stützle, 2014]



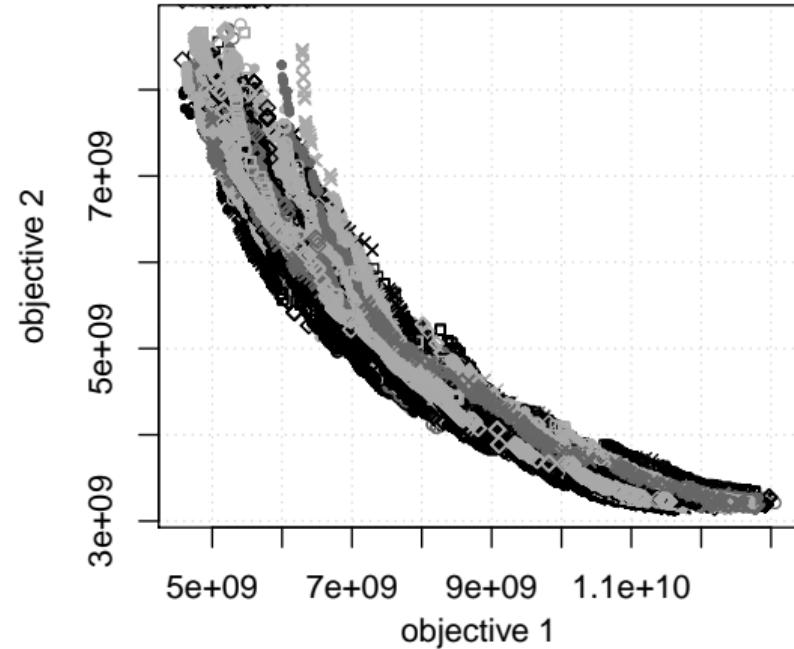
Is HV enough?

Algorithm configuration **A** (100 runs)



Mean HV = 0.920016

Algorithm configuration **B** (100 runs)

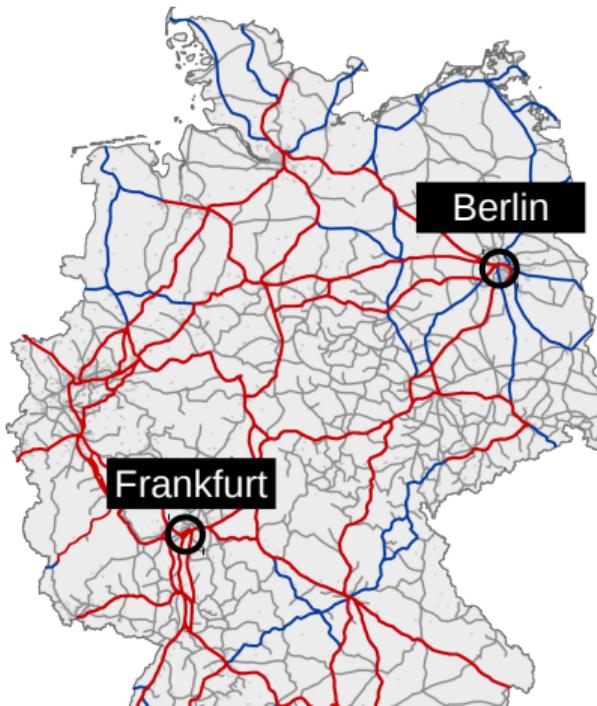


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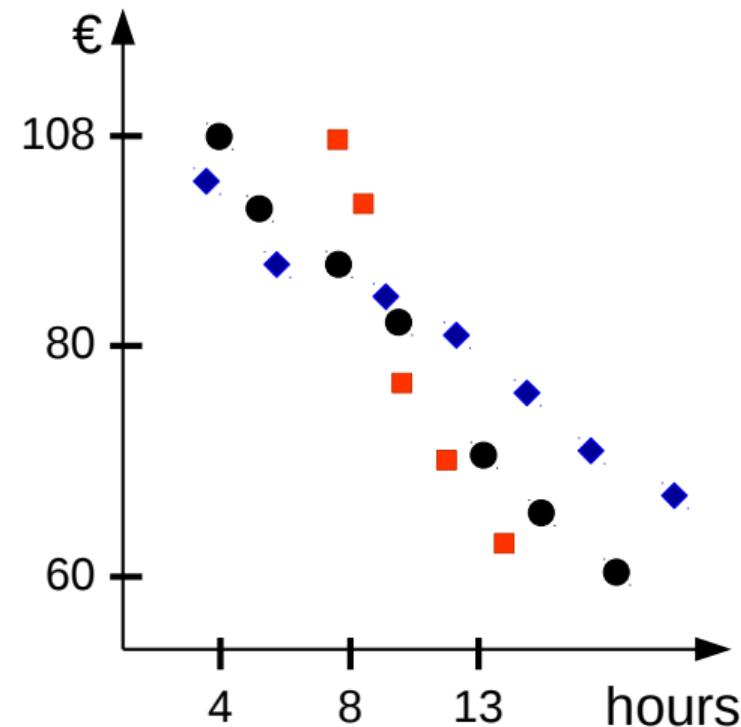
What are the differences between these two methods?

Is HV enough?

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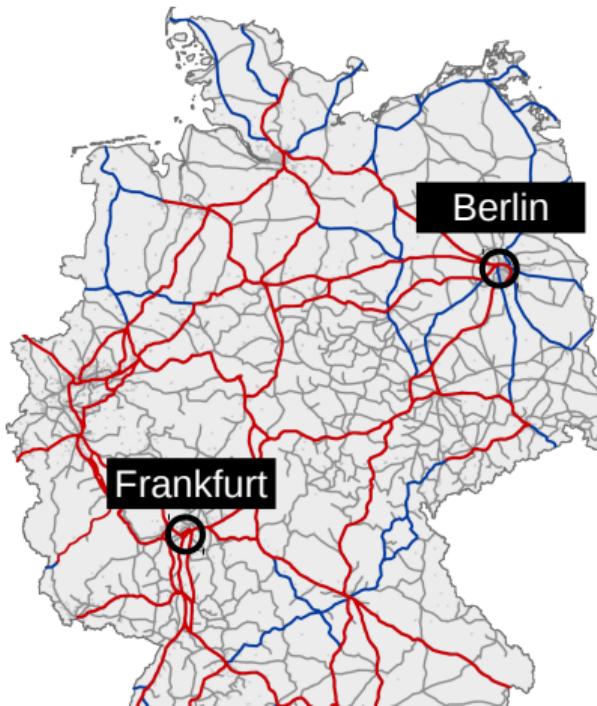


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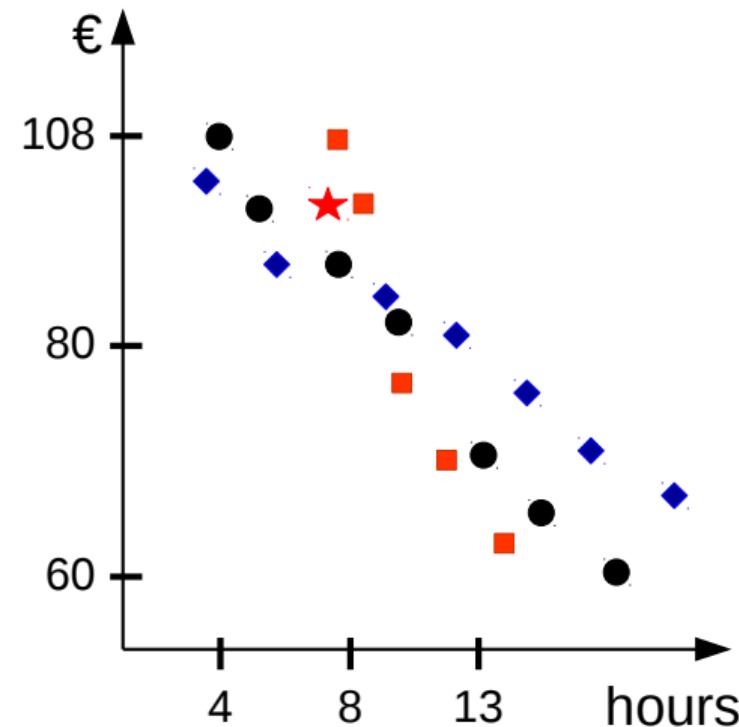


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- Probability of a random set \mathcal{A} *attaining* (weakly dominating) a particular point $\vec{z} = \vec{f}(x)$ in the objective space

$$\alpha_{\mathcal{A}}(\vec{z}) = \Pr\{\mathcal{A} \preceq \vec{z}\}$$

- Statistical distribution of the output (\mathcal{A}) of stochastic multi-objective optimizers
- ✗ The real attainment function is *unknown* but...

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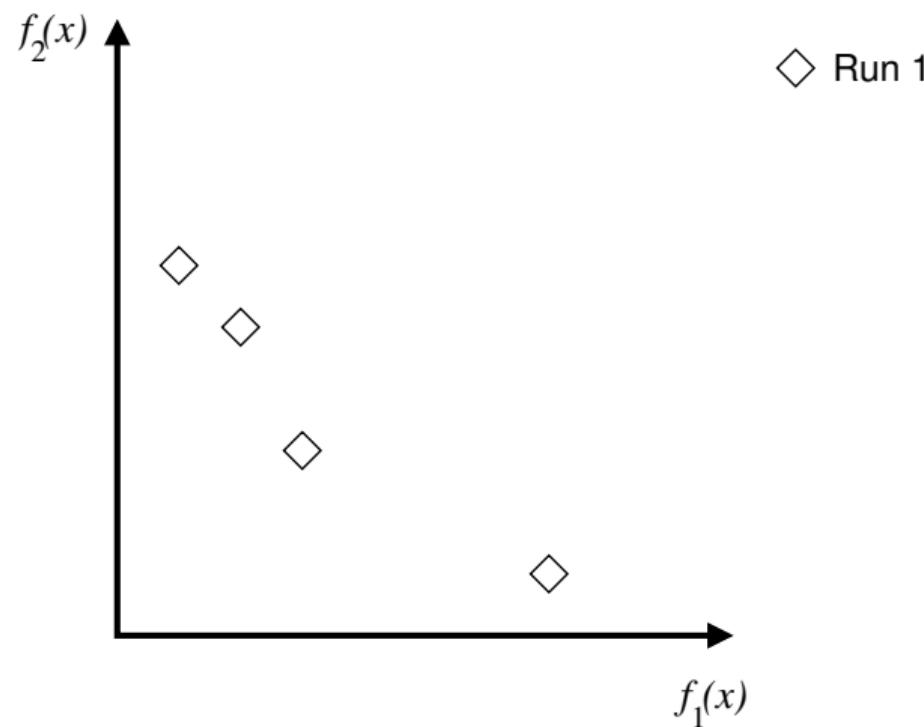
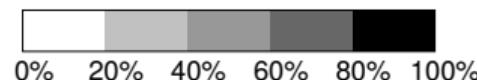
- Statistical distribution of the output (\mathcal{A}) of stochastic multi-objective optimizers
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- ✓ ... we can *estimate* it given $\{A_1, A_2, \dots\} \sim \mathcal{A}$:

Empirical attainment function (EAF)

The Empirical Attainment Function

[Grunert da Fonseca et al., 2001]

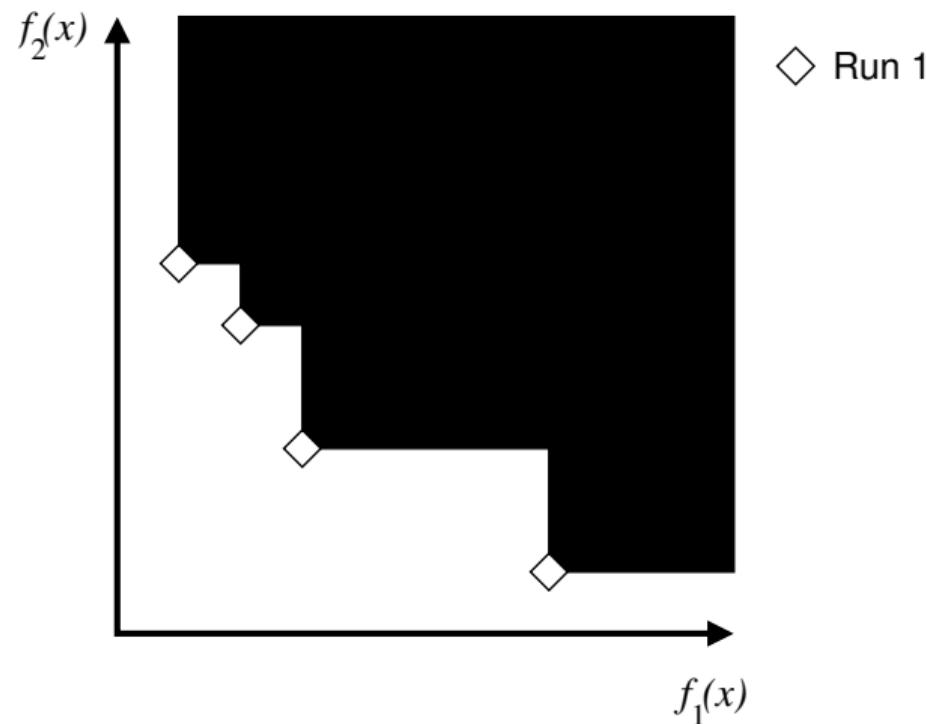
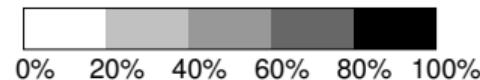
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The Empirical Attainment Function

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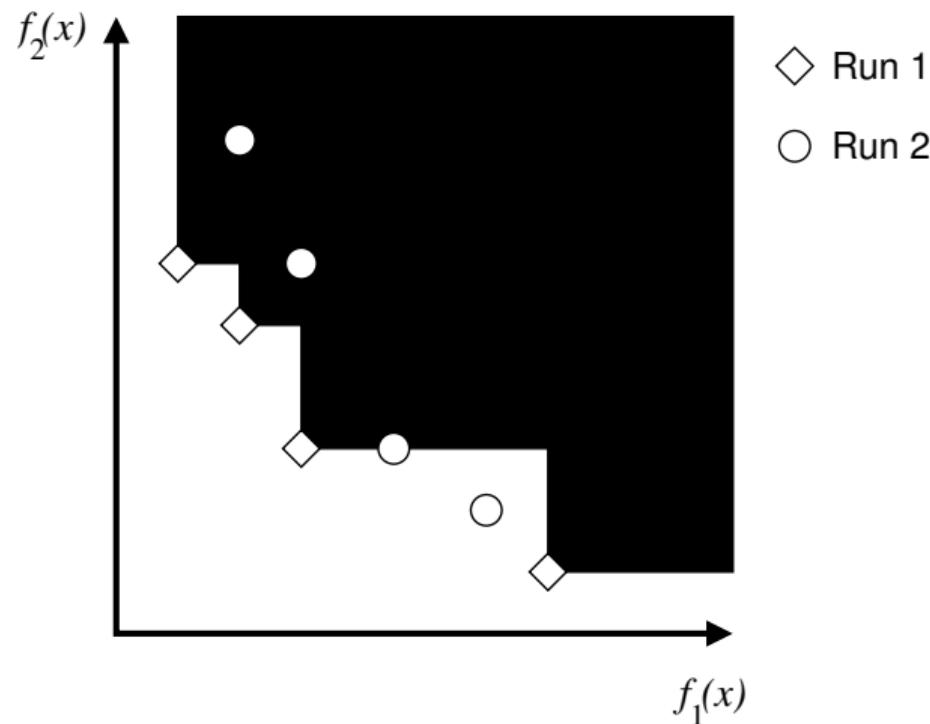
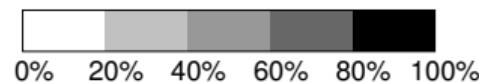
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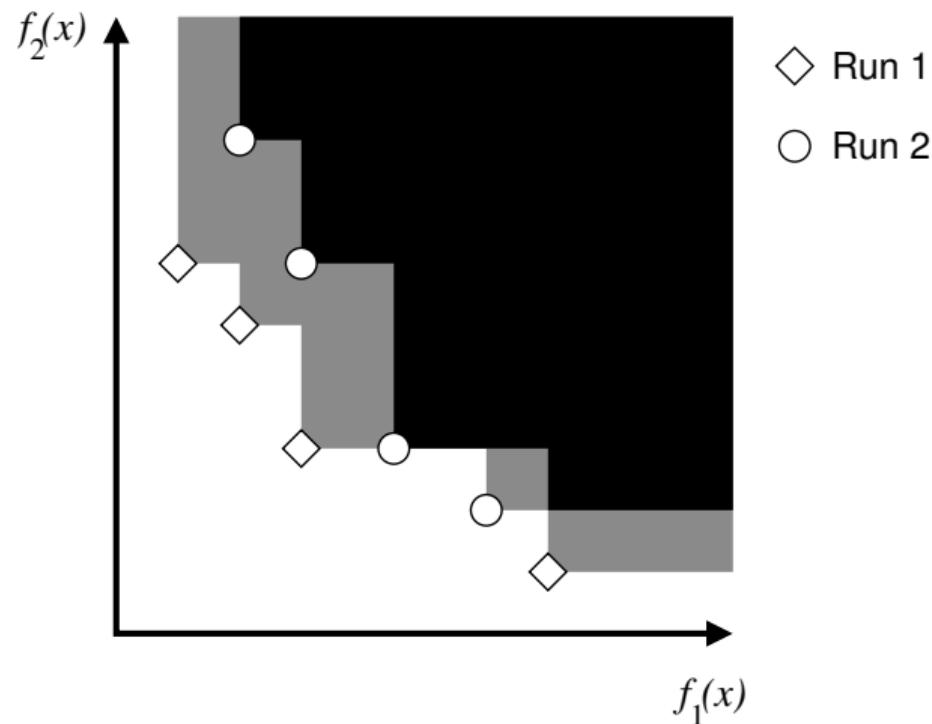
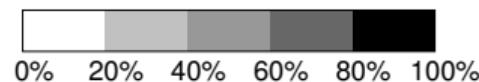
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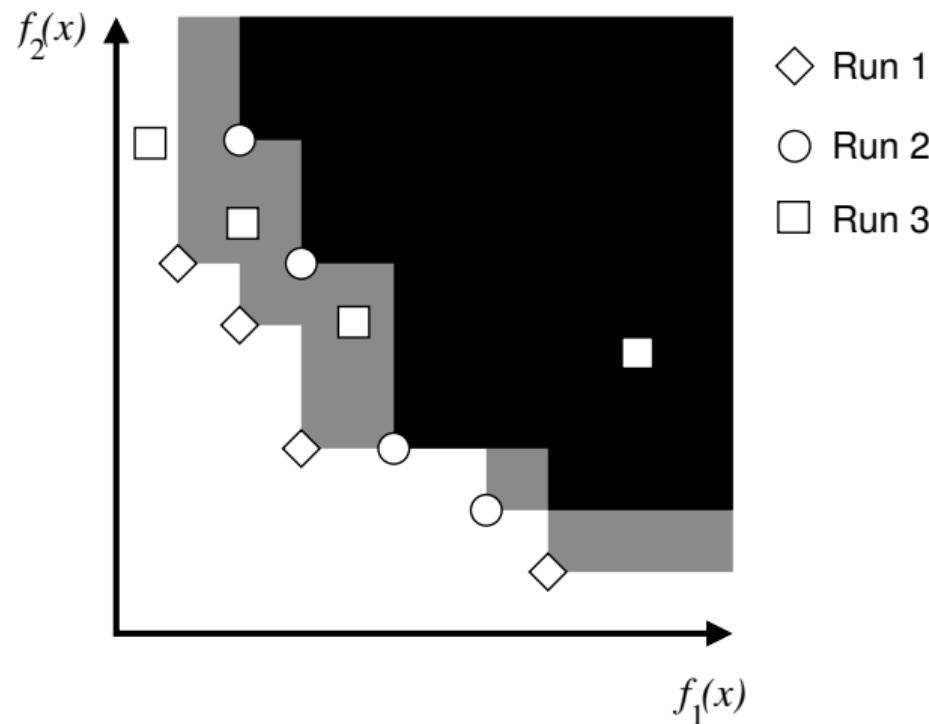
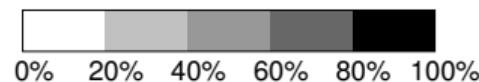
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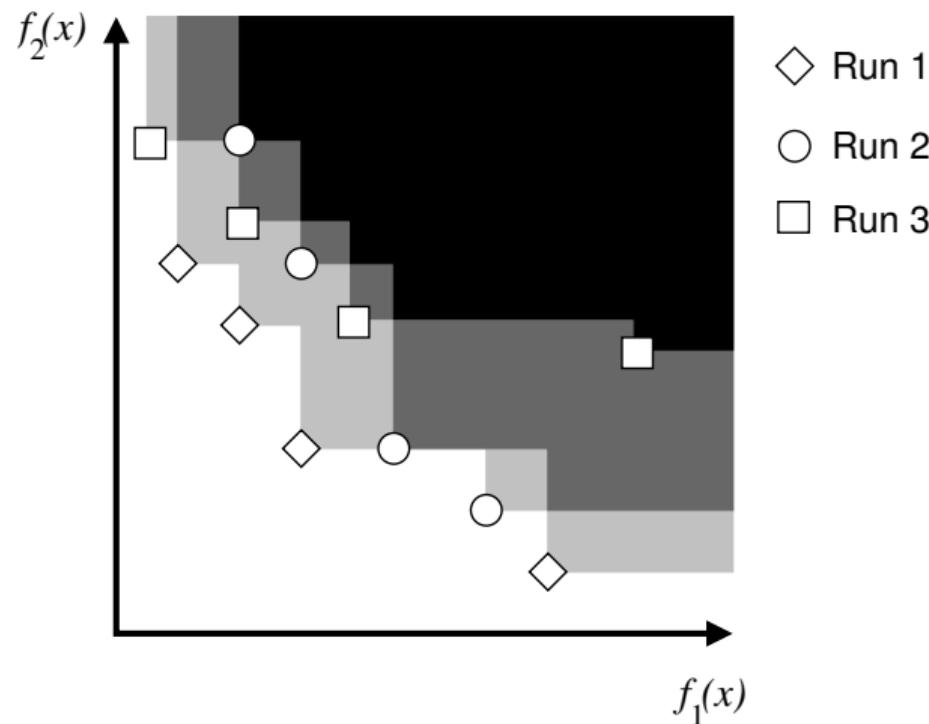
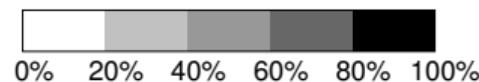
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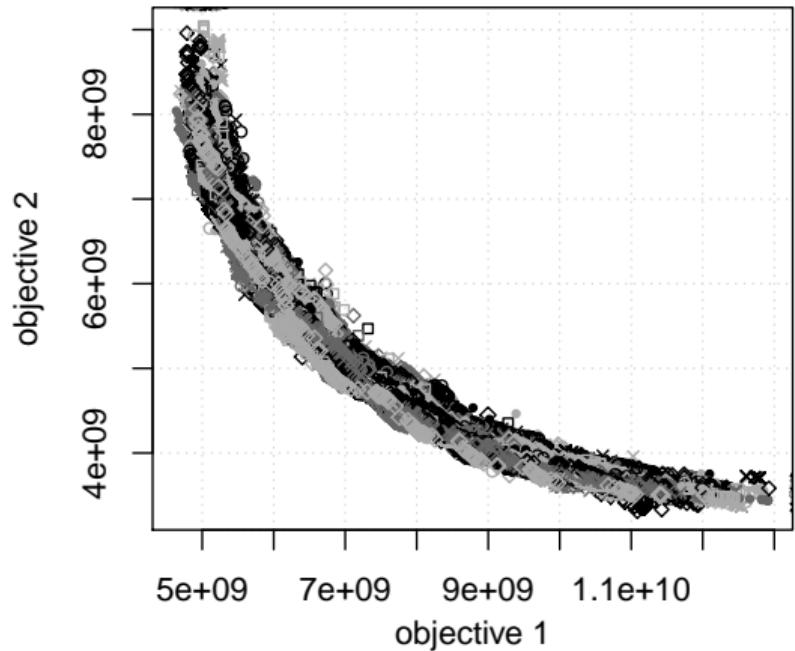
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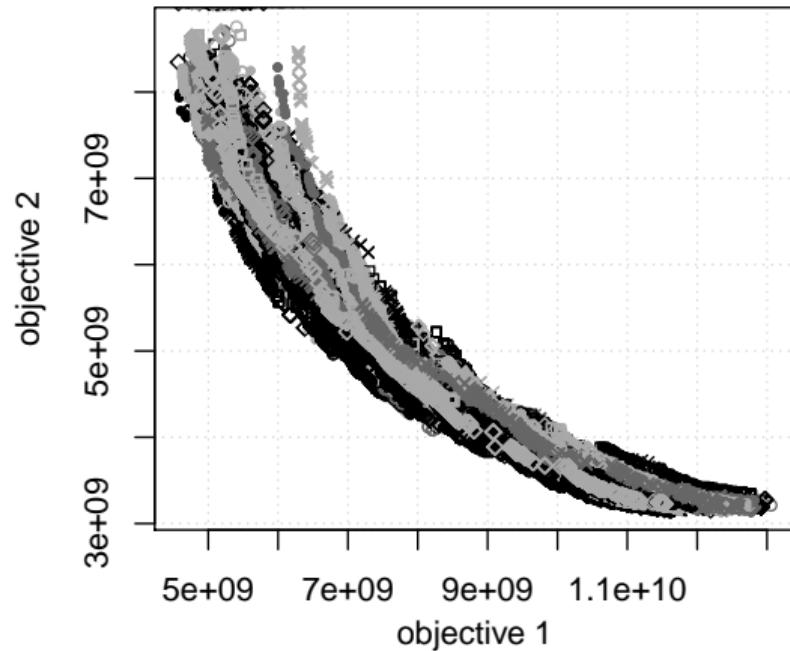
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Stochastic Nondominated Sets

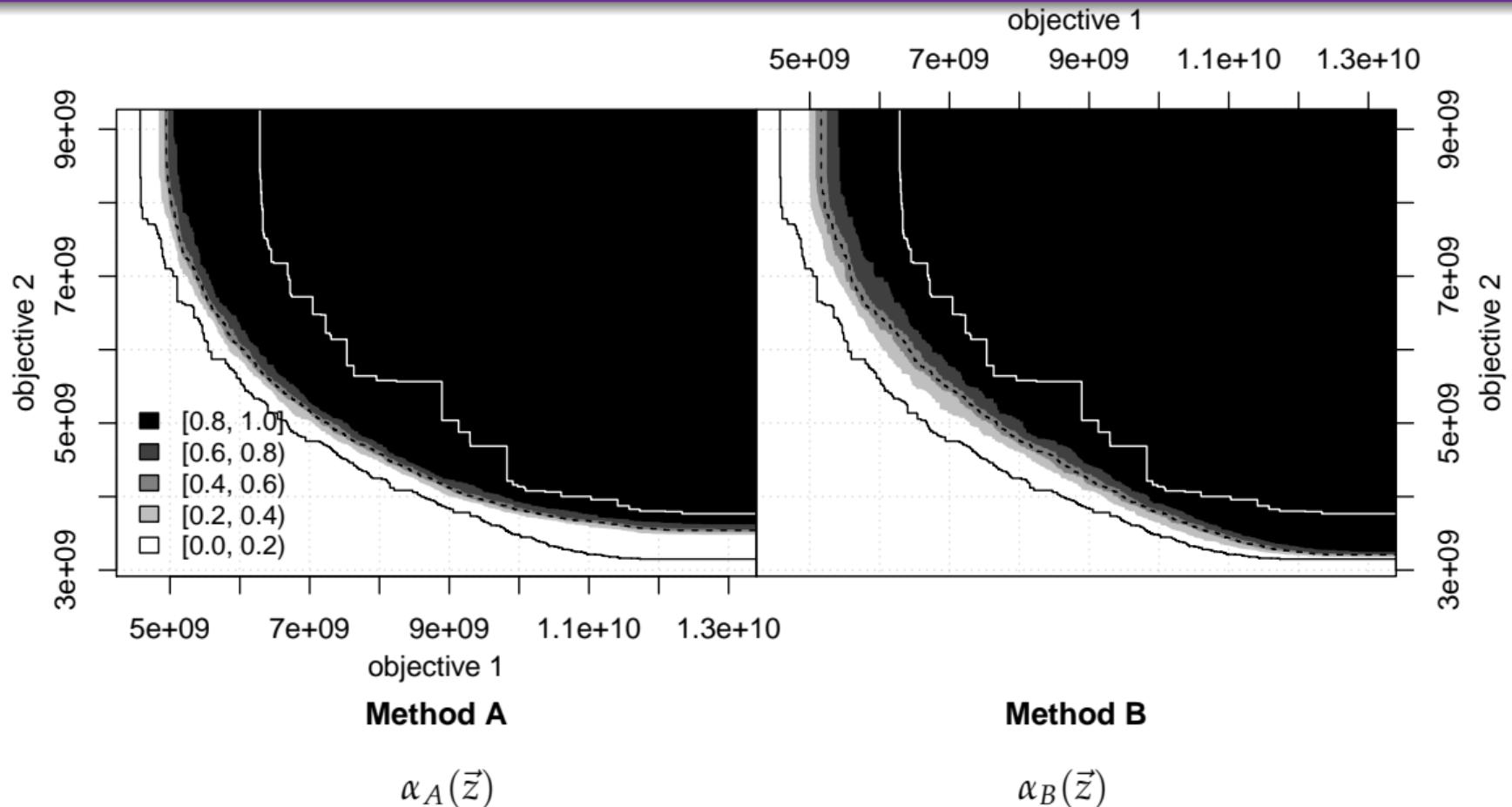


Algorithm **A** (100 runs)



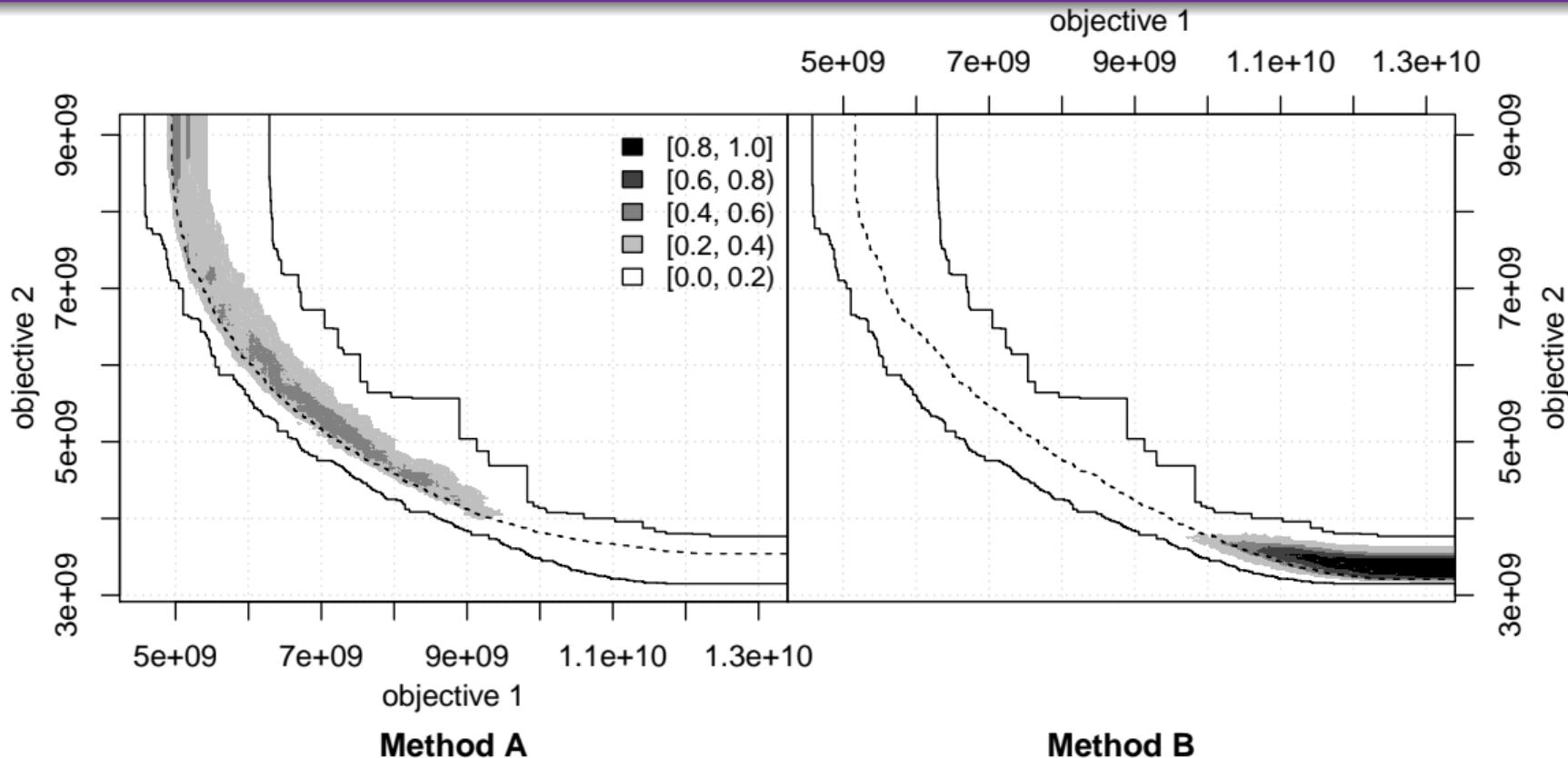
Algorithm **B** (100 runs)

Comparing two algorithms: Side-by-side EAFs



Comparing two algorithms: EAF differences

[López-Ibáñez et al., 2010]



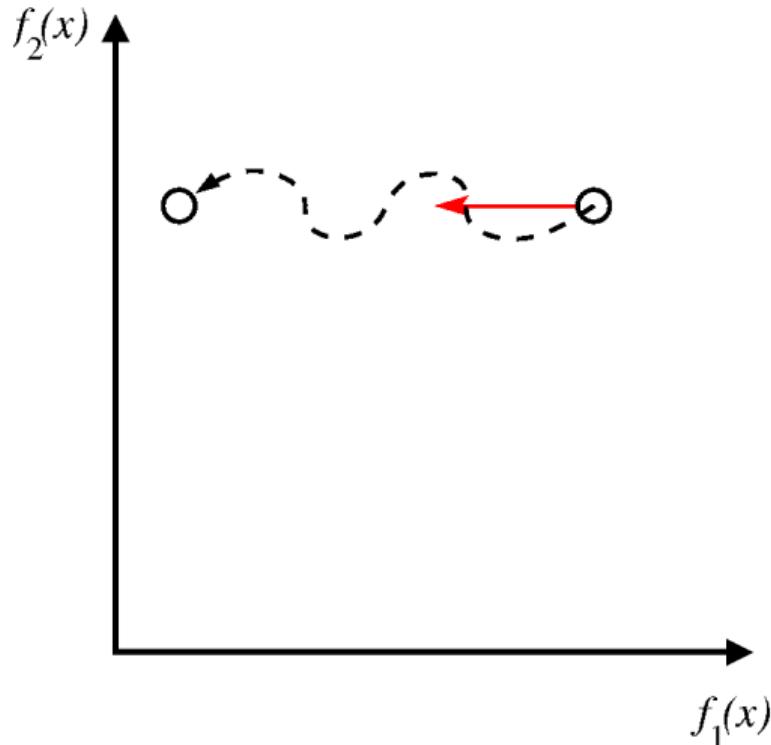
$$\max\{\alpha_A(\vec{z}) - \alpha_B(\vec{z}), 0\}$$

$$\max\{\alpha_B(\vec{z}) - \alpha_A(\vec{z}), 0\}$$

- Scalarize the bQAP using a weight $\lambda \in [0, 1]$

$$f_\lambda(x) = \lambda \cdot f_1(x) + (1 - \lambda) \cdot f_2(x)$$

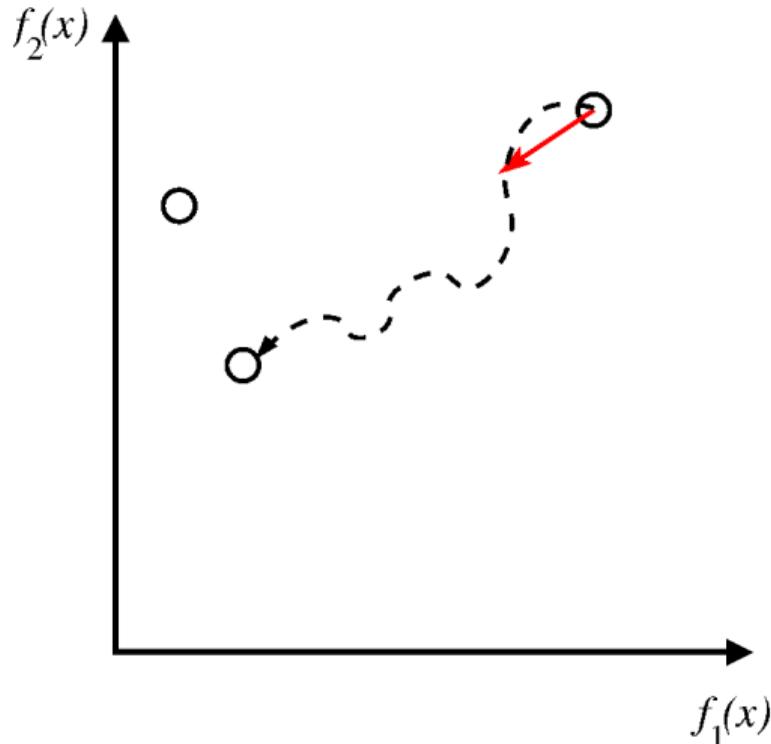
- Solve each f_λ with RoTS [Taillard, 1991]
stopping after $\ell \cdot n$ iterations



- Scalarize the bQAP using a weight $\lambda \in [0, 1]$

$$f_\lambda(x) = \lambda \cdot f_1(x) + (1 - \lambda) \cdot f_2(x)$$

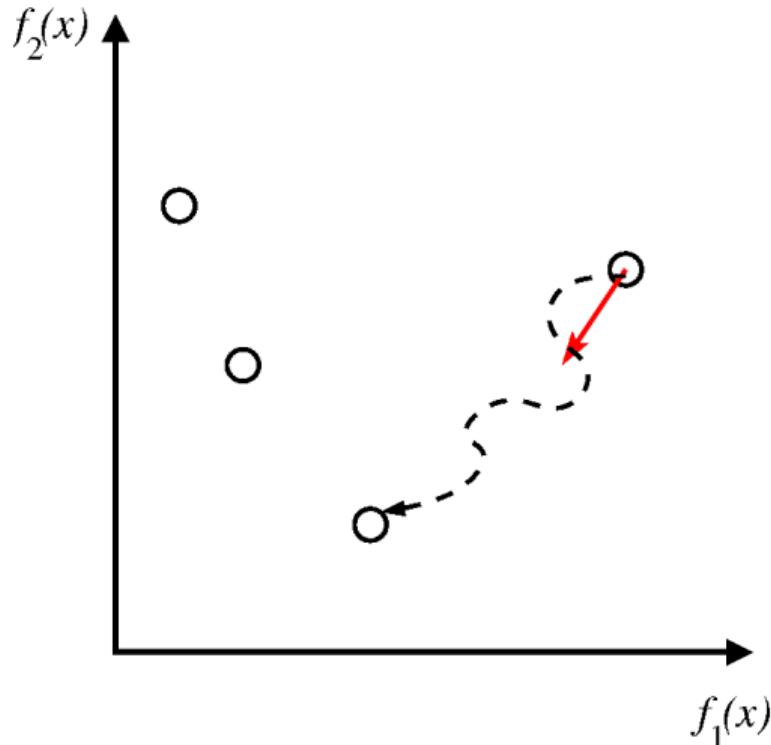
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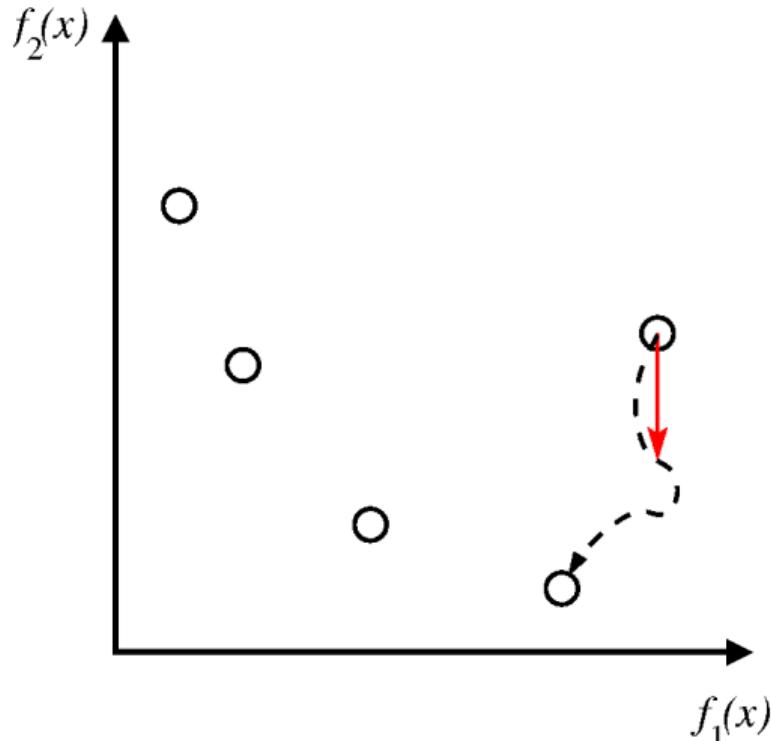
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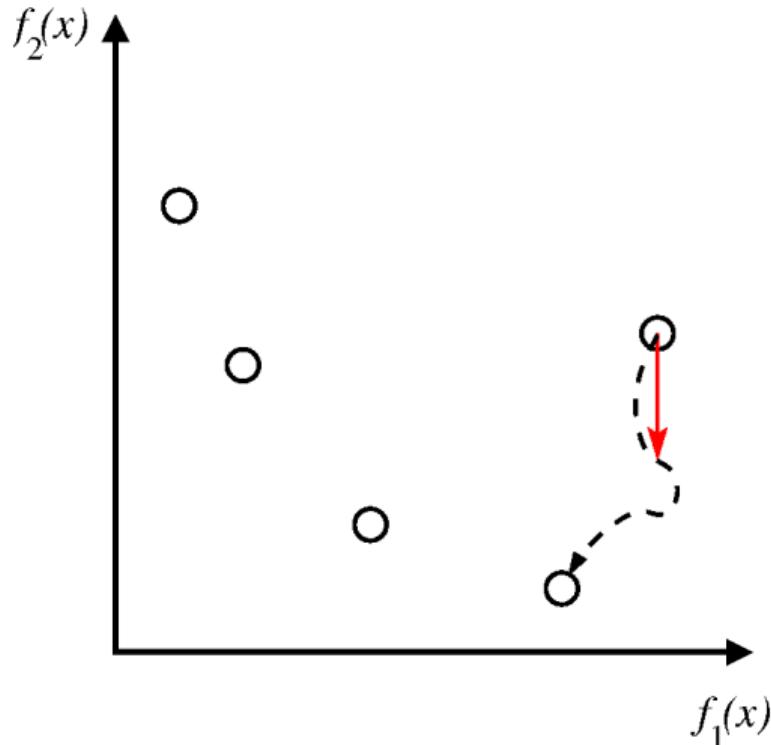
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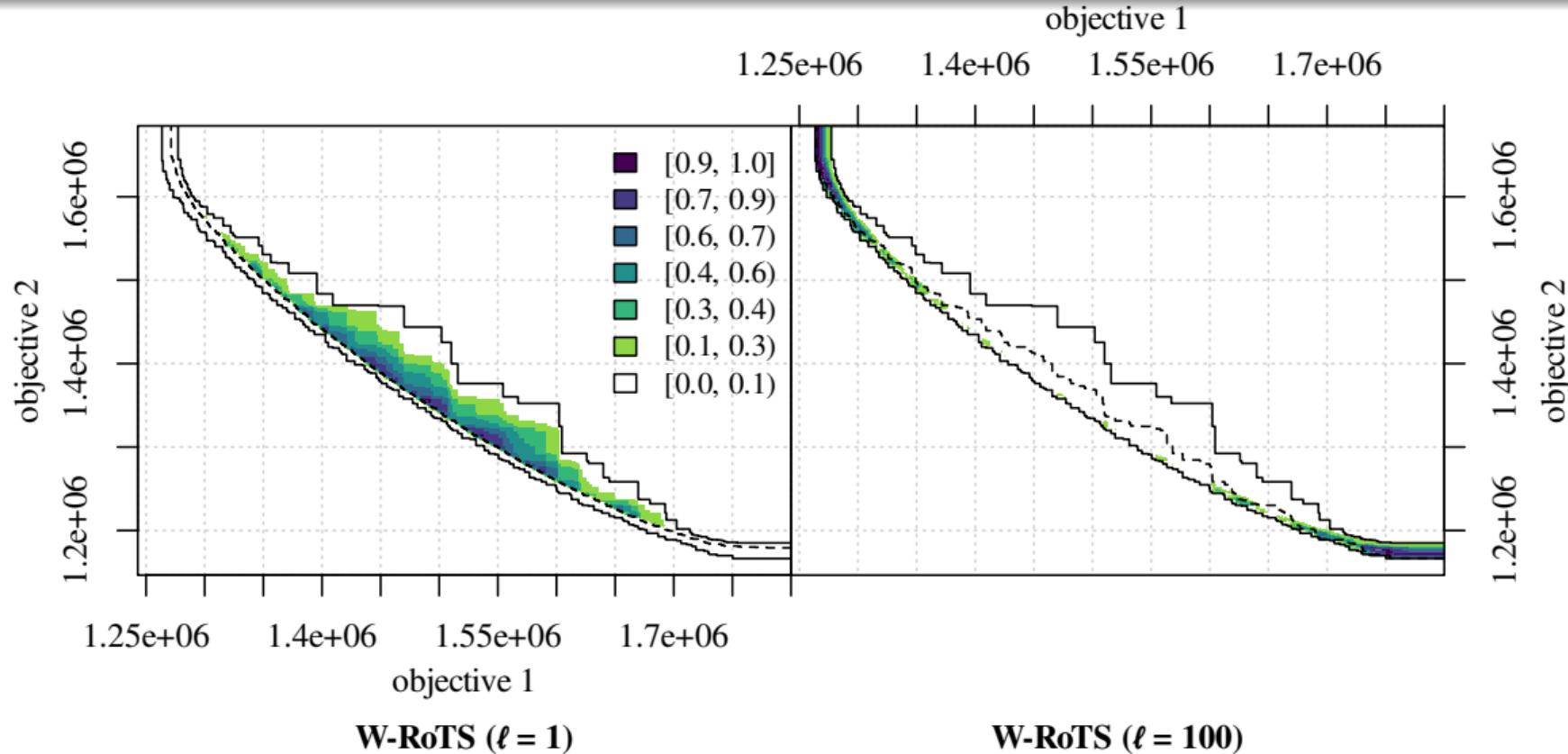
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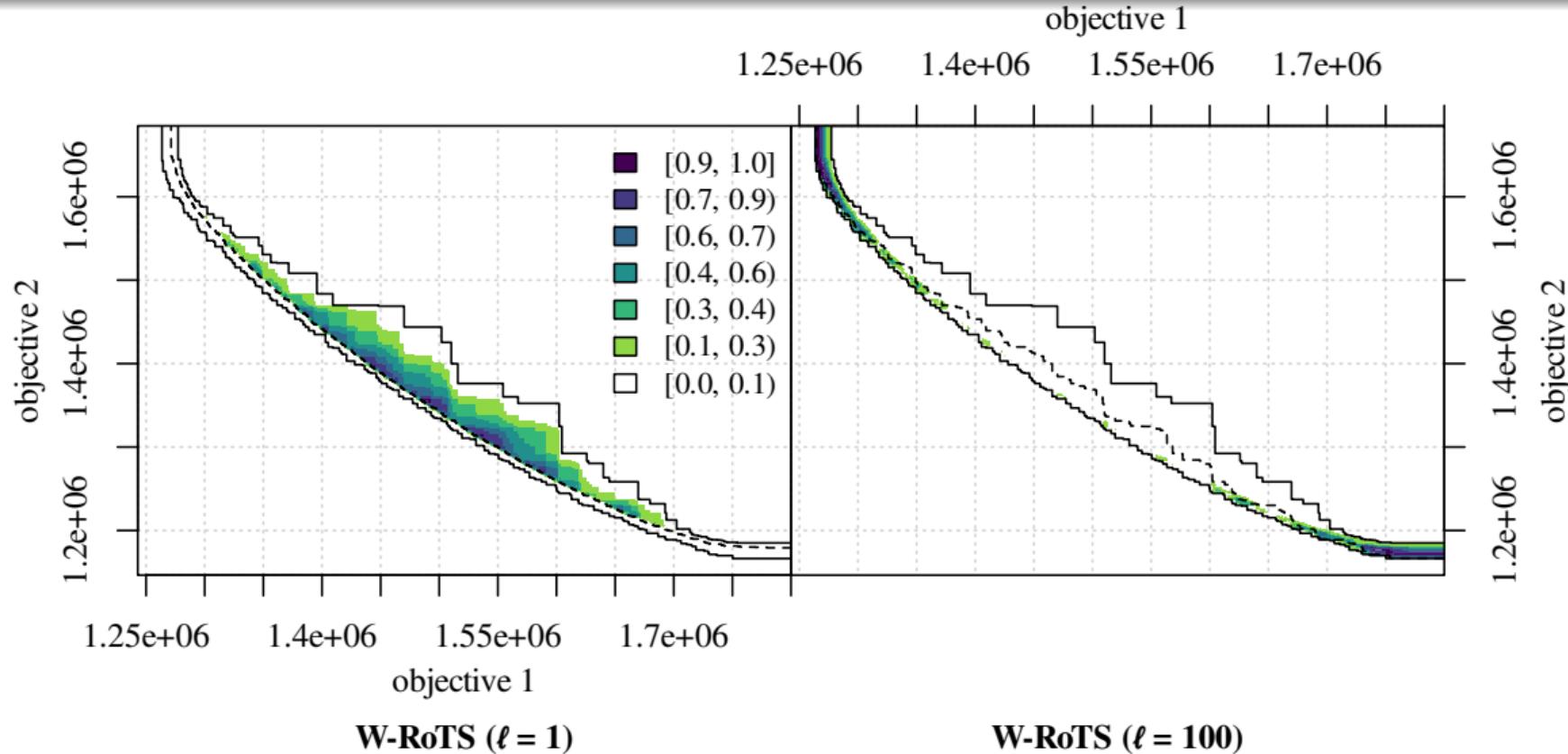


Best value of ℓ ?

Tuning the value of ℓ in W-RoTS



Tuning the value of ℓ in W-RoTS



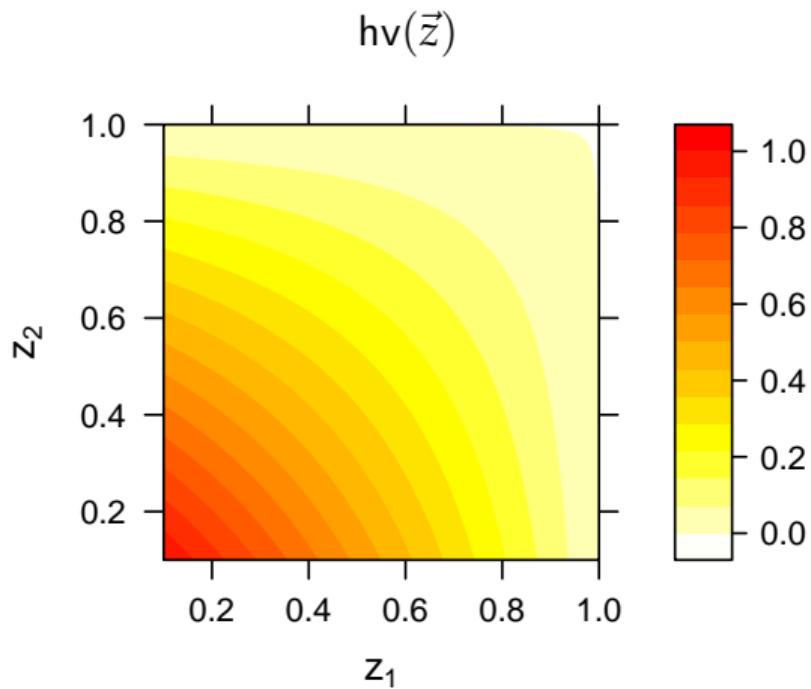
HV assumes a preference that may be different from the DM's !



Bias the computation of the HV by assigning weights to regions of the objective space

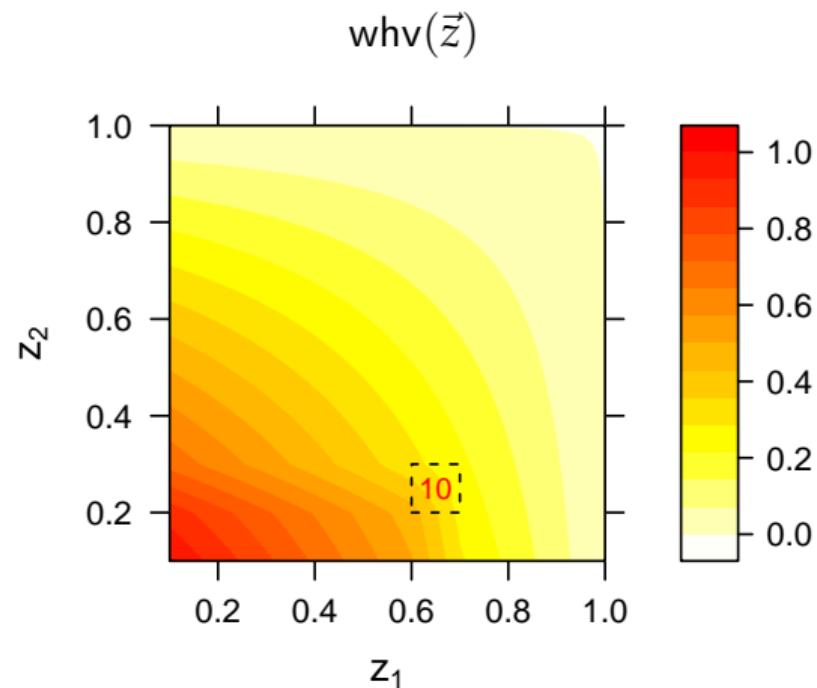
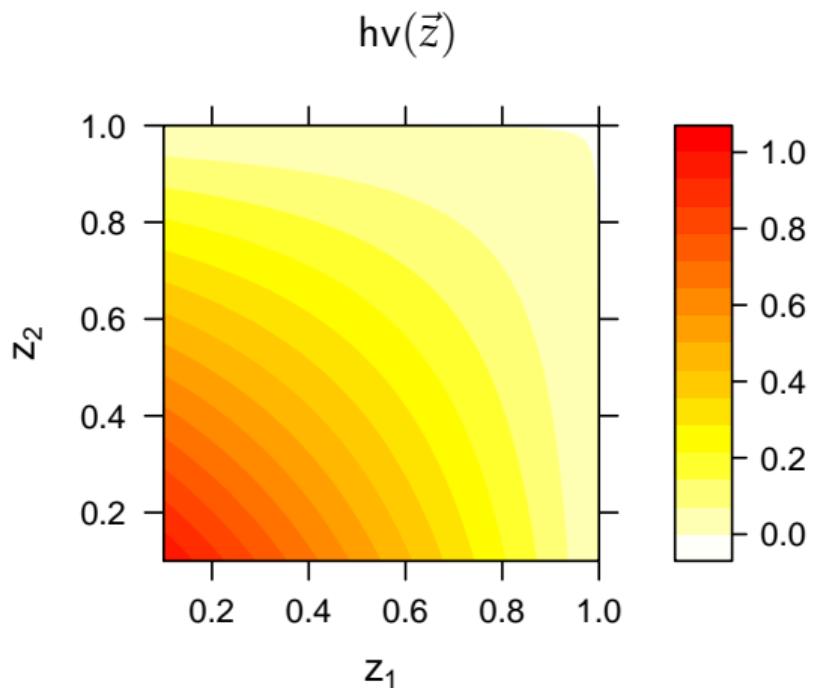


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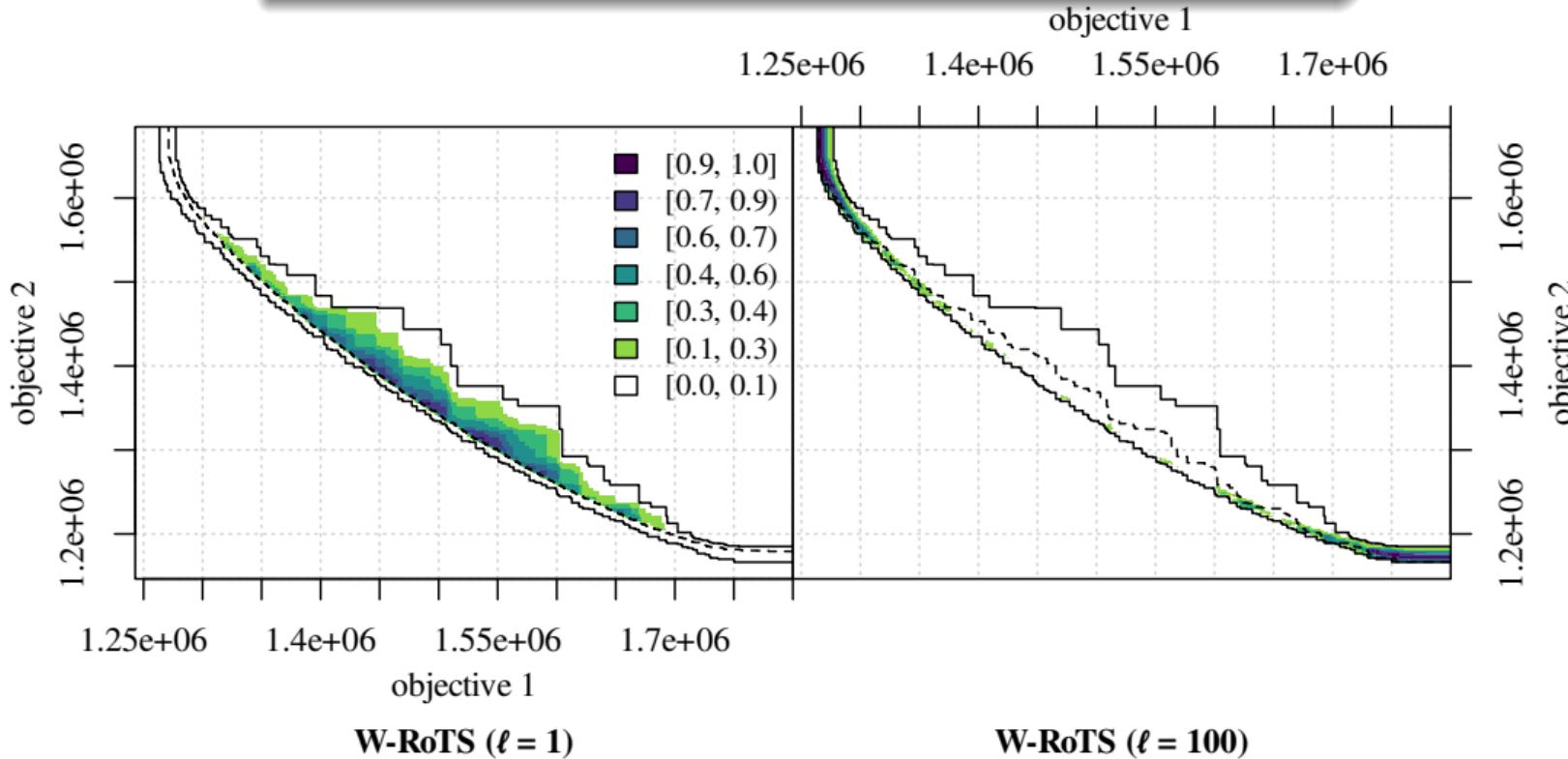
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Interactively Tuning the value of ℓ in W-RoTS

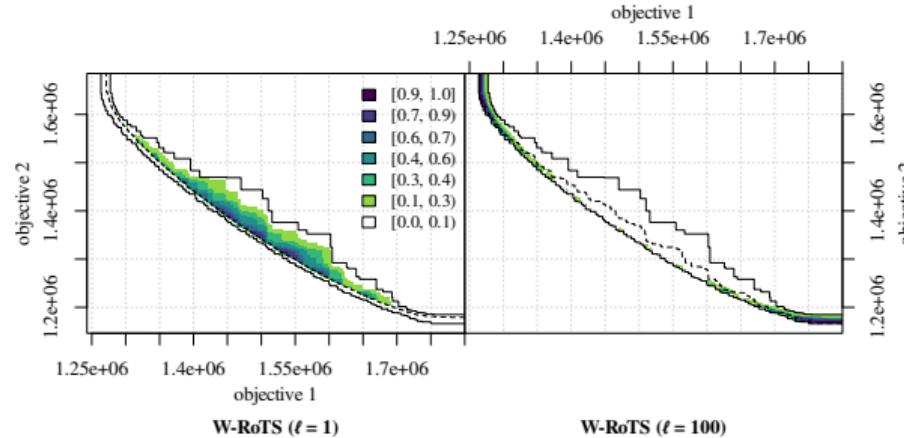


Convert EAF differences into weighted hypervolume



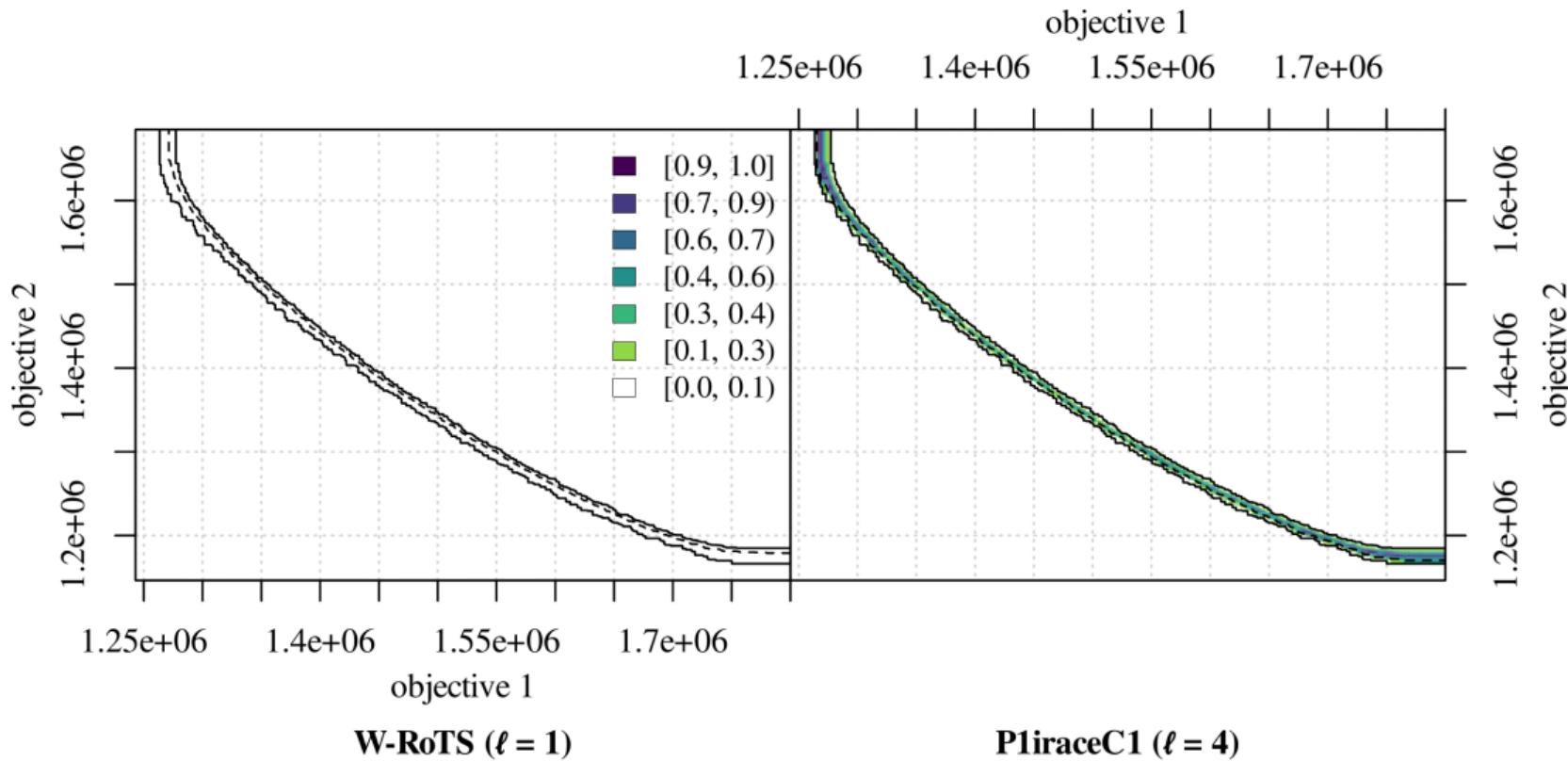
Interactively Tuning the value of ℓ in W-RoTS

💡 Use this weighted hypervolume to guide the automatic algorithm configuration of a bi-objective optimizer

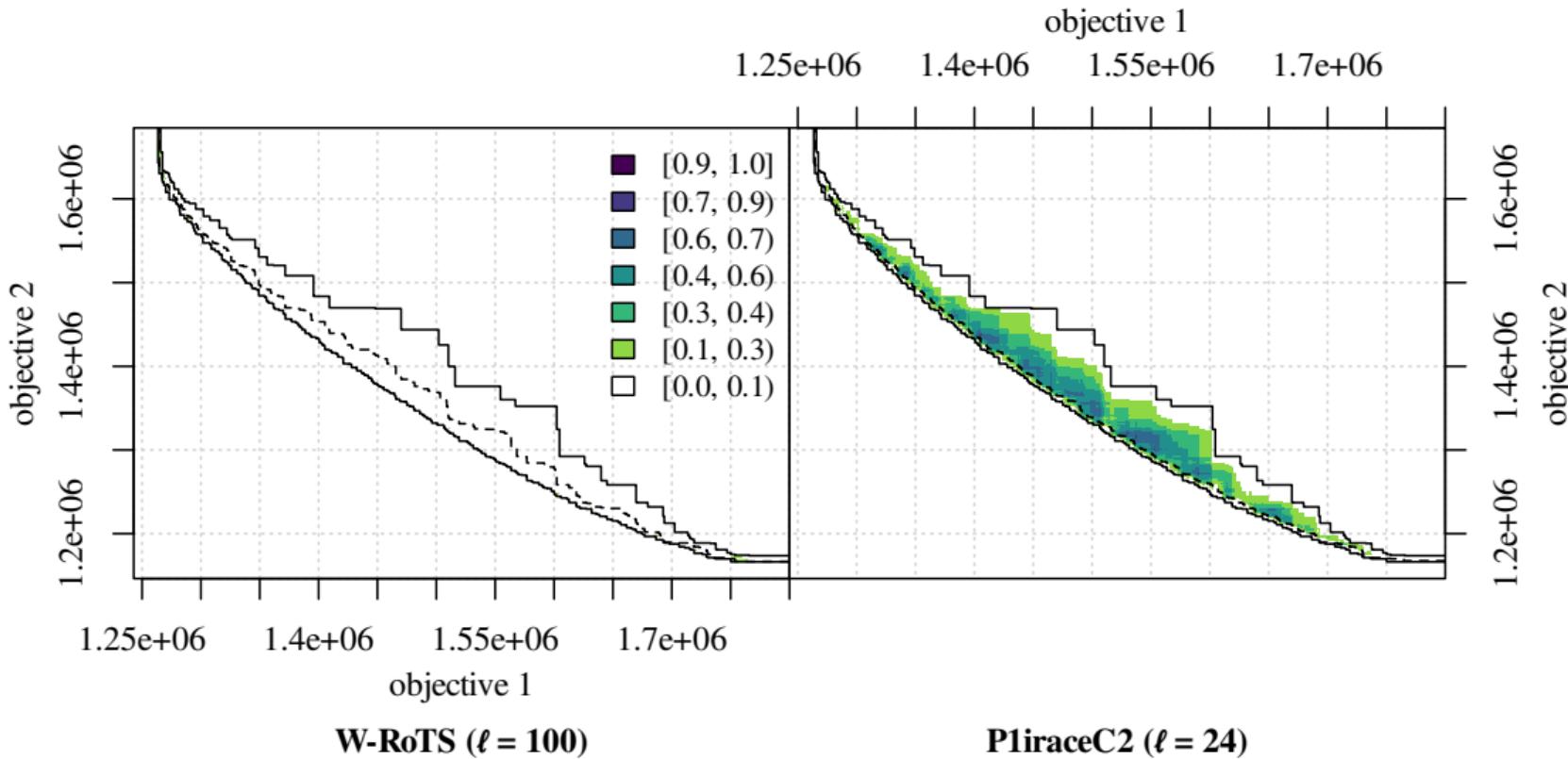


- (1) The DM chooses one side, e.g., $\ell = 1$
- (2) Compute regions \mathcal{R} in favour
- (2) Create $HV_{\mathcal{R}}^W(\cdot)$ based on positive EAF differences
- (3) Tune $\ell \in [1, 200]$ using irace guided by $HV_{\mathcal{R}}^W(\cdot)$ (budget = 500 runs of W-RoTS)

Interactively Tuning the value of ℓ in W-RoTS



Interactively Tuning the value of ℓ in W-RoTS

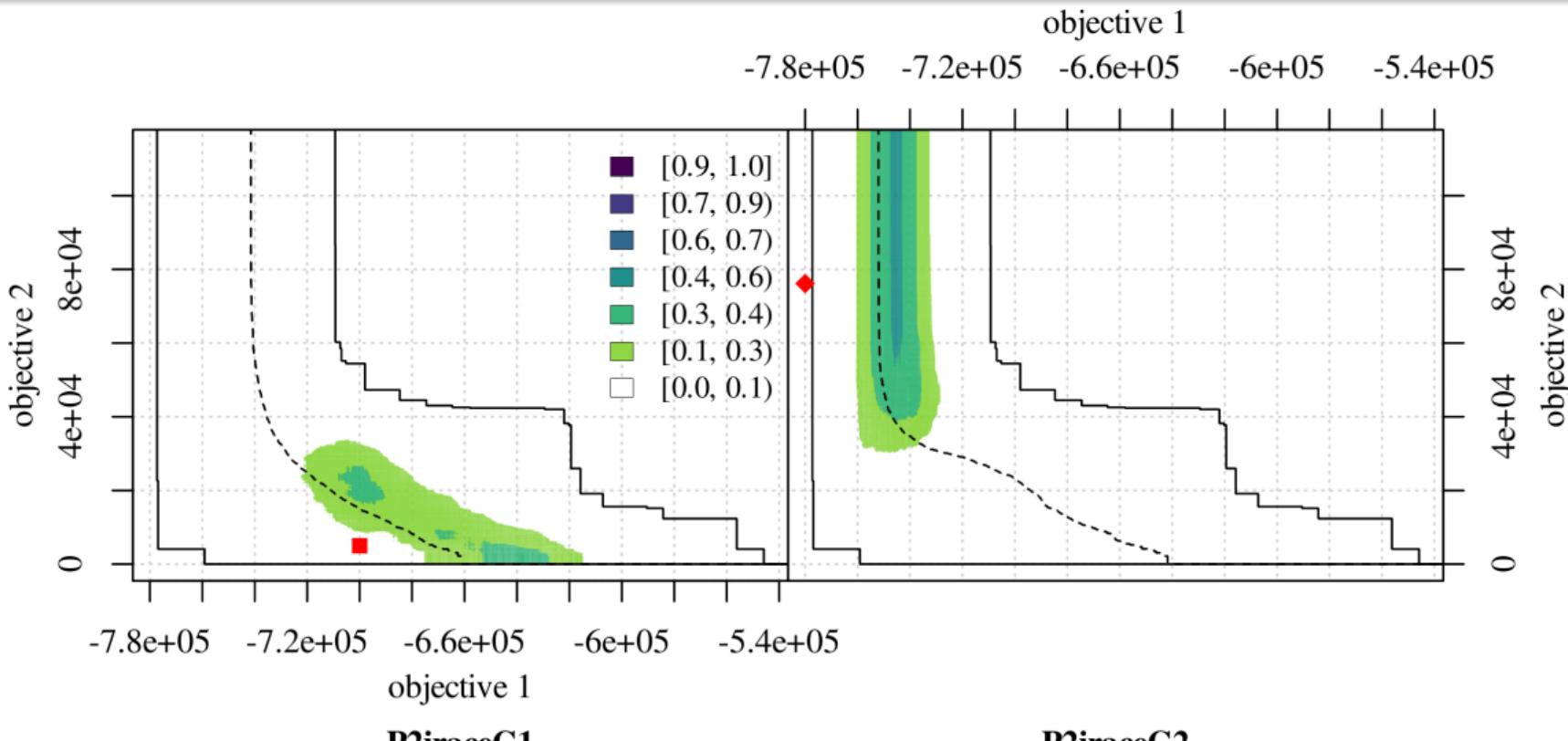


irace is clearly focusing on different regions

- Bi-objective multi-product capacitated production planning problem within a failure-prone batch manufacturing system specialised on cleaning products
- Custom MOEA + discrete event simulator
- MOEA has 4 categorical, 2 real and 2 integer parameters

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- Custom MOEA + discrete event simulator
- MOEA has 4 categorical, 2 real and 2 integer parameters
- Tuning procedure:
 - (1) Run irace guided by *unweighted* HV (budget = 1000 MOEA runs)
 - (2) Select 2 configurations showing the largest EAF differences
 - (3) Show EAF differences to DM and ask to choose a side
 - (4) Compute regions \mathcal{R} in favour of chosen side
 - (5) Create $HV_{\mathcal{R}}^w(\cdot)$ based on chosen regions
 - (6) Continue running irace guided by $HV_{\mathcal{R}}^w(\cdot)$ (budget = 1000 MOEA runs)

Interactive Tuning Procedure

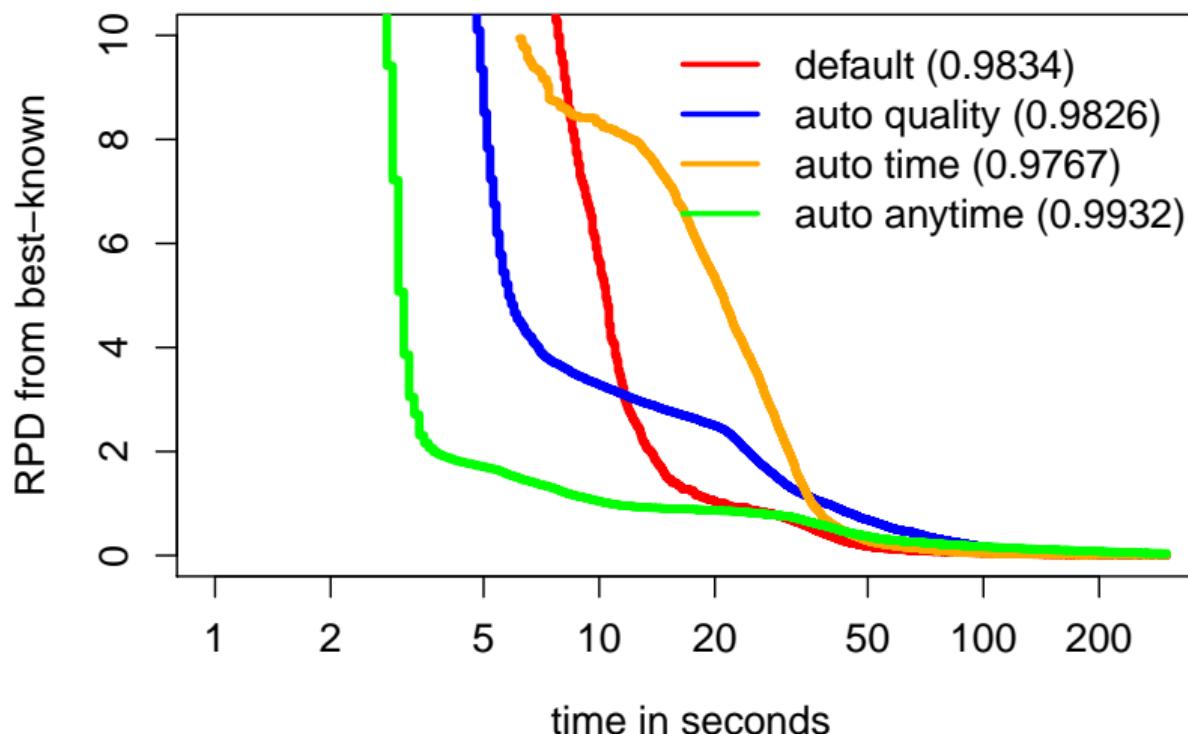


irace is clearly focusing on different regions

Not Only Bi-objective Algorithms

- SCIP (single-objective MIP solver, 200 parameters)
- **Goal:** improve anytime behavior using irace

[López-Ibáñez & Stützle, 2014]



Conclusions and Future Work

- Automatic configuration and design of multi-objective algorithms
 - ➡ This is the past! Use it now! [Bezerra et al., 2020b]
- irace + EAF diffs + weighted hypervolume
 - = *Interactive configuration and design of bi-objective optimizers*
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- ✓ More control of the DM over the resulting algorithm design

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TODO list:

- ? How to aggregate over subsequent DM interactions?
- ? How to aggregate preferences over very different problem instances?
- ? How to interact with ≥ 3 objectives?

Multi-objective Bayesian Optimization

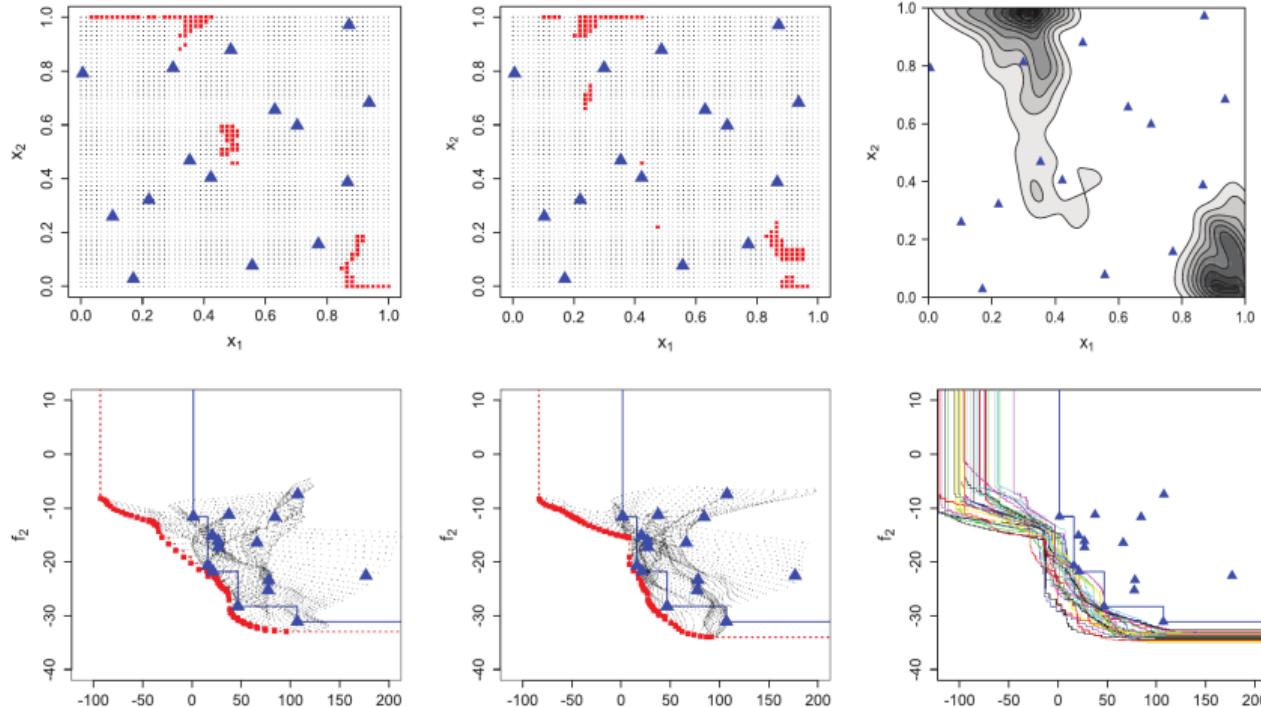


M. Binois, D. Ginsbourger, & O. Roustant.

Quantifying uncertainty on Pareto fronts with Gaussian process conditional simulations.

European Journal of Operational Research, 243(2):386–394, 2015

👉 Conditional Pareto fronts = Nondominated sets sampled from the GPs



Multi-objective Bayesian Optimization

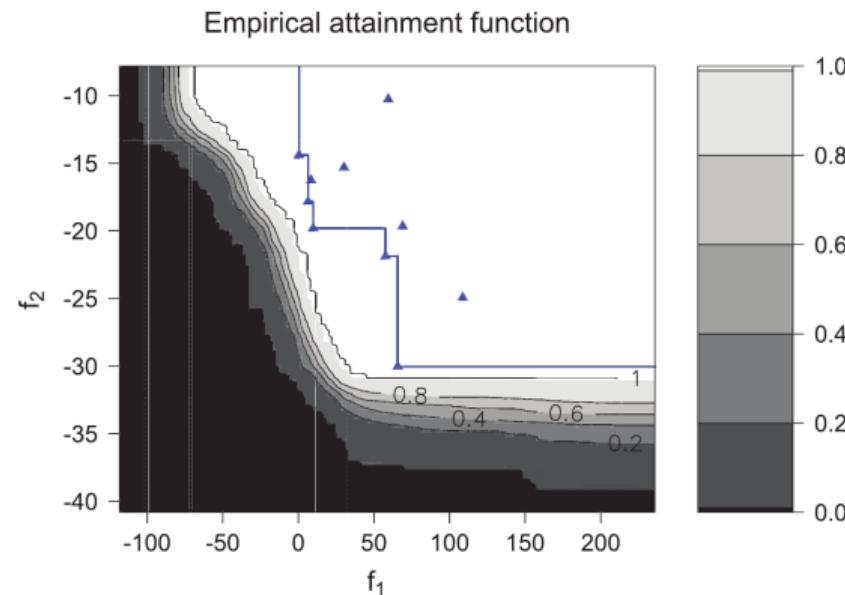


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☞ Conditional Pareto fronts \Rightarrow EAF

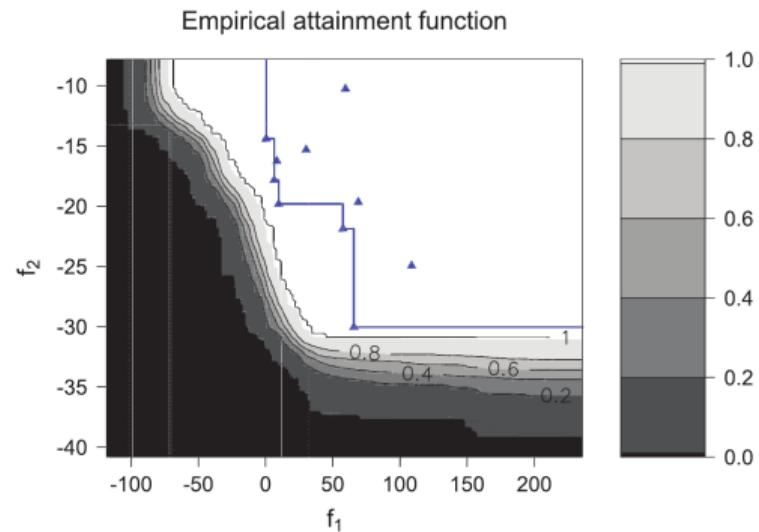
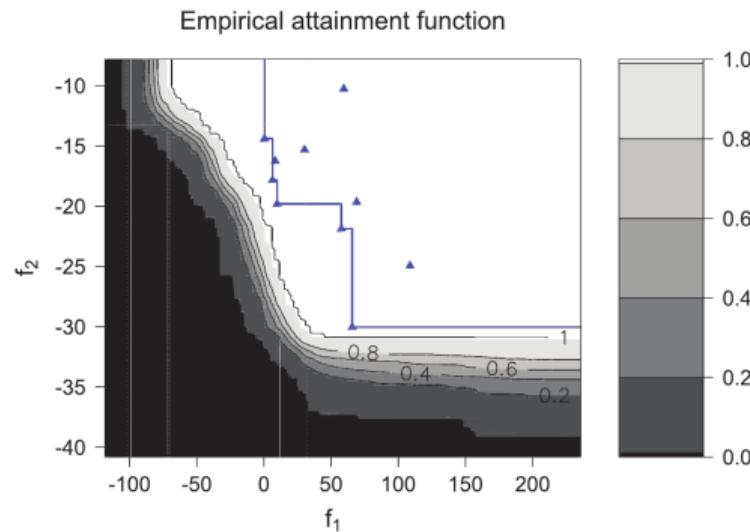


Interactive Hyper-parameter Tuning of Multi-objective Bayesian Optimizers

- Conditional Pareto fronts \Rightarrow EAF
- Alternative hyper-parameter settings: kernels, AF, optimizer, ...

 EAF differences \Rightarrow Let the DM choose which uncertainty is preferable

\Rightarrow Tune accordingly



QUIT LIVING IN THE PAST



THE FUTURE IS TODAY

Incorporating Decision-Maker's Preferences into the Automatic Configuration of Bi-objective Optimisation Algorithms

Manuel López-Ibáñez

manuel.lopez-ibanez@manchester.ac.uk

<http://lopez-ibanez.eu>

The Joint Lectures on Evolutionary Algorithms (JoLEA)

15 February 2023



The University of Manchester
Alliance Manchester Business School



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Goal 1: Flexible

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- Implementation of (Elitist) Iterated Racing in R
 - Goal 1: Flexible
 - Goal 2: Easy to use
- R package available at [CRAN](#) (GNU/Linux, Windows, OSX)
- Use it through the command-line: (see `irace --help`)

```
irace --max-experiments 1000 --param-file parameters.txt
```
- ✓ No knowledge of R needed
- Google group: <https://groups.google.com/forum/#!forum/irace-package>

An overview of applications of irace

- Parameter tuning
 - Exact MIP solvers: CPLEX, SCIP [López-Ibáñez & Stützle, 2014]
 - Single-objective optimization metaheuristics
 - Multi-objective optimization metaheuristics
 - Anytime optimization (improve time-quality trade-offs)
 - Command-line flags of GCC compiler [Pérez Cáceres et al., 2017]
- Automatic algorithm design
 - From a flexible framework of algorithm components
 - From a grammar description
- Machine learning (AutoML)
 - Automatic model selection for survival analysis [Lang et al., 2014]
 - **mlr** R package [Bischl et al., 2013, 2016]
- Design of control software for robots [Francesca et al., 2015]
- *Theoretical research* [Friedrich et al., 2018; Dang & Doerr, 2019]

EAF differences \Rightarrow Weighted HV



Use EAF differences to define the weighted HV

\mathcal{R} : “regions” with EAF differences in favor of the choice made by the DM

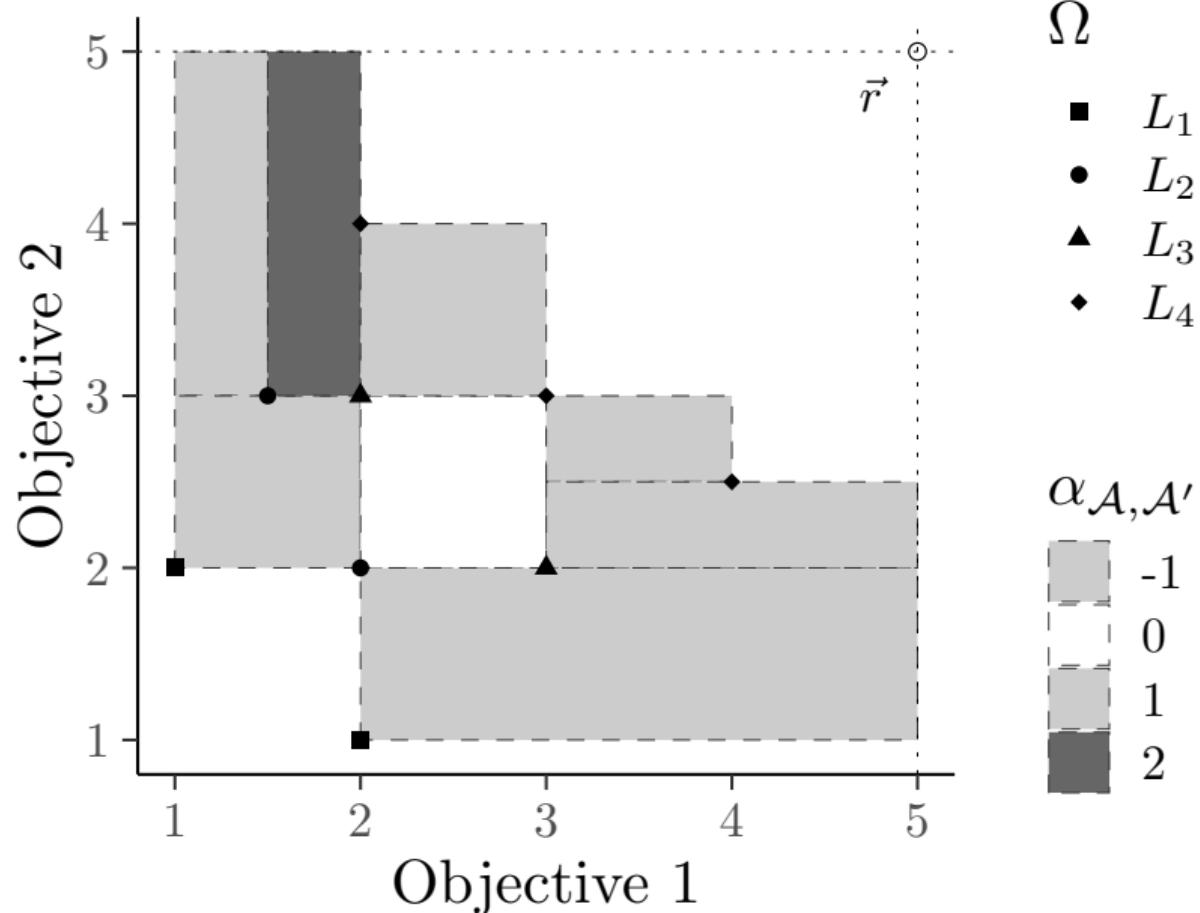
A : a new approximation front

$$HV^w(A) = HV(A) + HV_{\mathcal{R}}^w(A) \cdot \beta$$

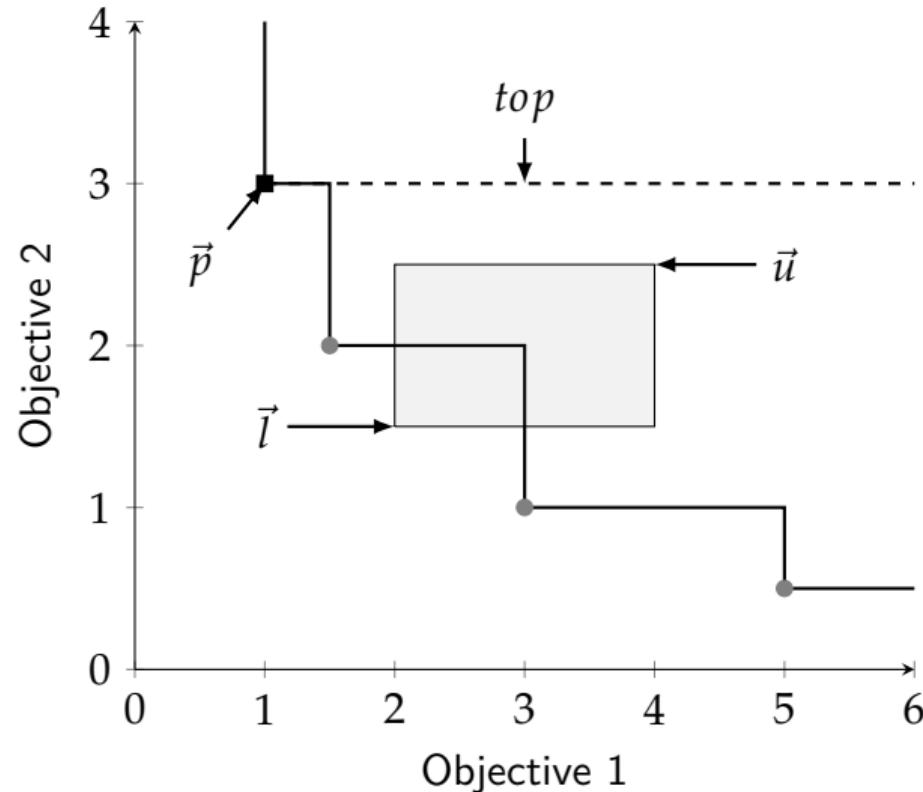
where $\beta = (r_1 - f_1^{\min}) \cdot (r_2 - f_2^{\min}) \cdot \varphi$

where $\varphi \in [0, 1]$ is a scaling factor

Computation of regions from EAF differences

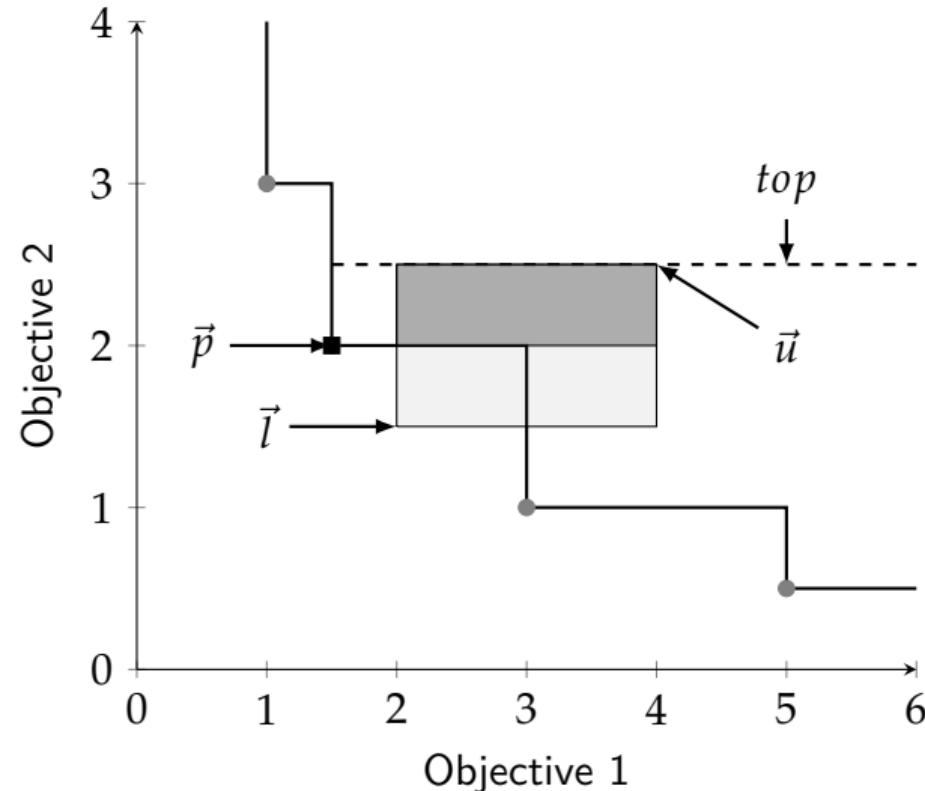


From EAF differences (\mathcal{R}) to $HV_{\mathcal{R}}^w(A)$



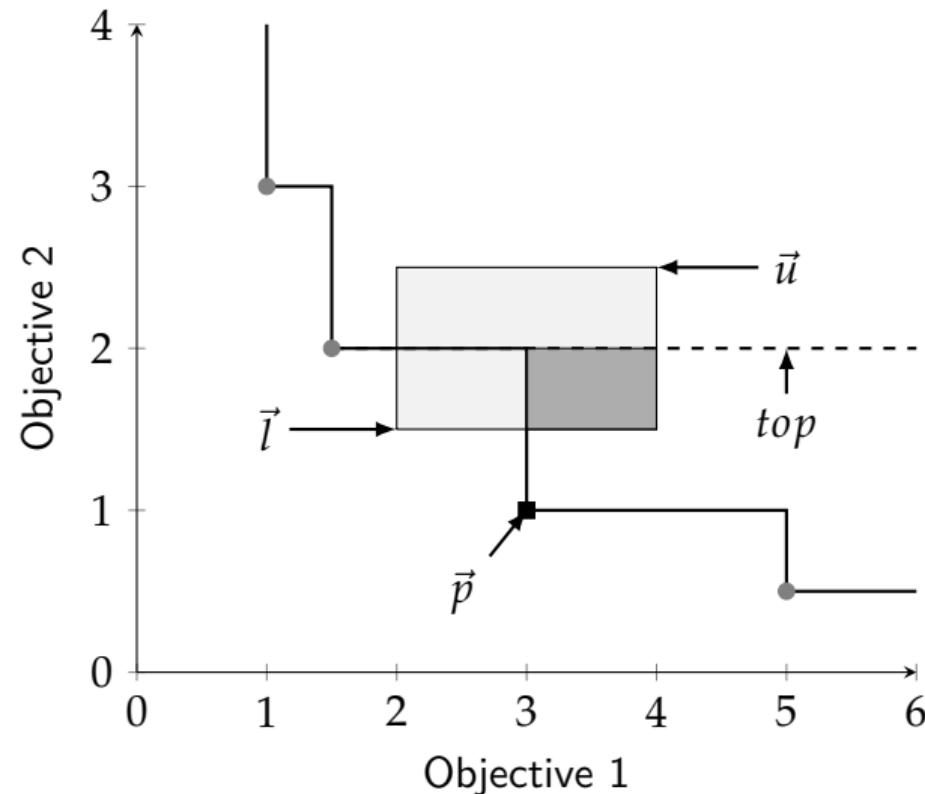
Case #1

From EAF differences (\mathcal{R}) to $HV_{\mathcal{R}}^w(A)$



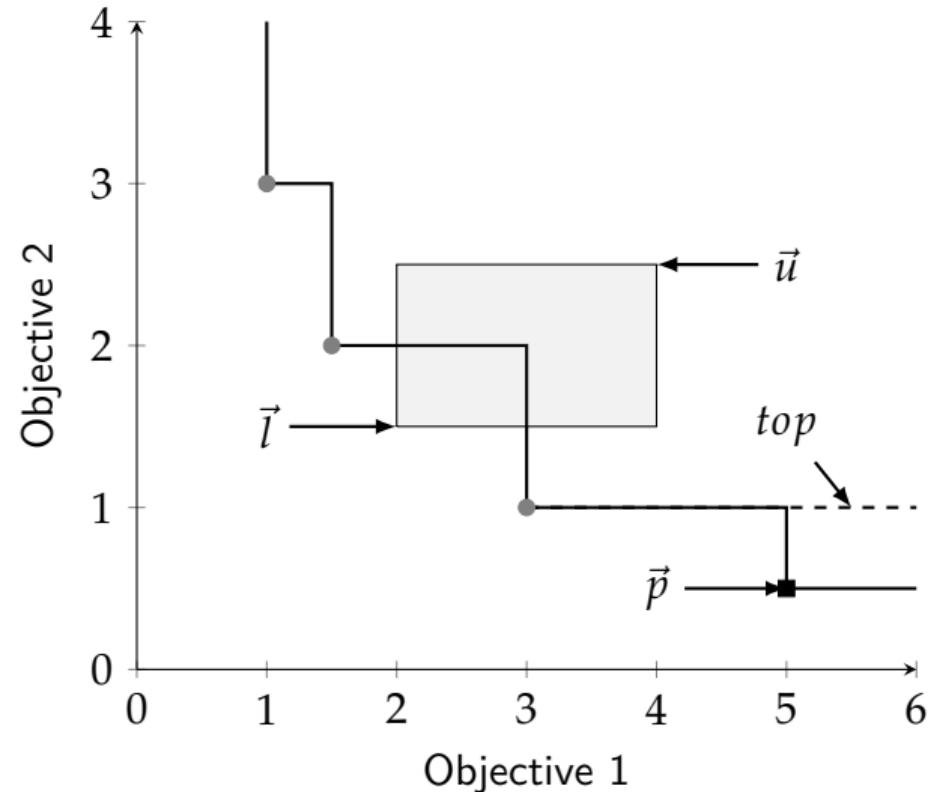
Case #2 bounded by u_2

From EAF differences (\mathcal{R}) to $HV_{\mathcal{R}}^w(A)$



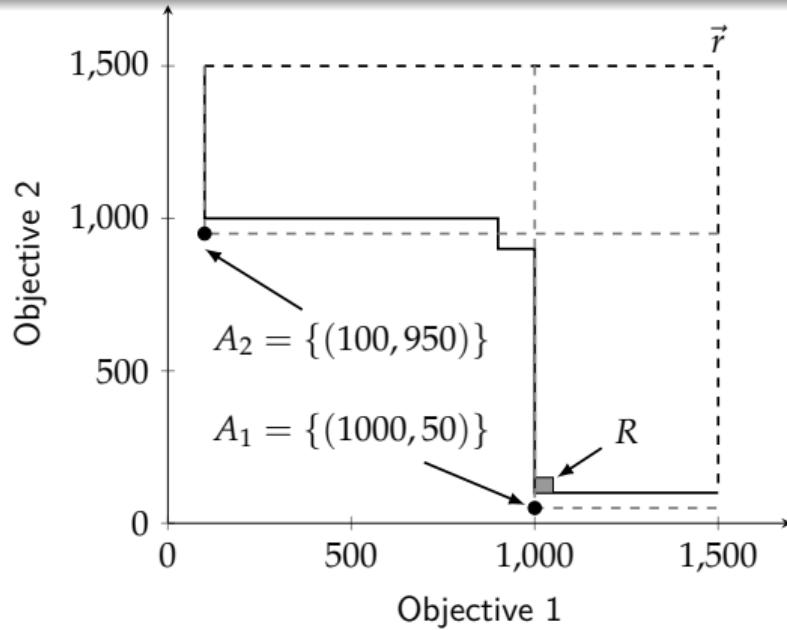
Case #2 bounded by top

From EAF differences (\mathcal{R}) to $HV_{\mathcal{R}}^w(A)$



Case #3

Example of the effect of β



- If $\beta = 1$,
then $HV^w(A_1) = 730000 < HV^w(A_2) = 770000$
- If $\beta = 0.5 \cdot (r_1 - f_1^{\min}) \cdot (r_2 - f_2^{\min})$
then $HV^w(A_1) = 2813225000 > HV^w(A_2) = 770000$

Largest EAF differences

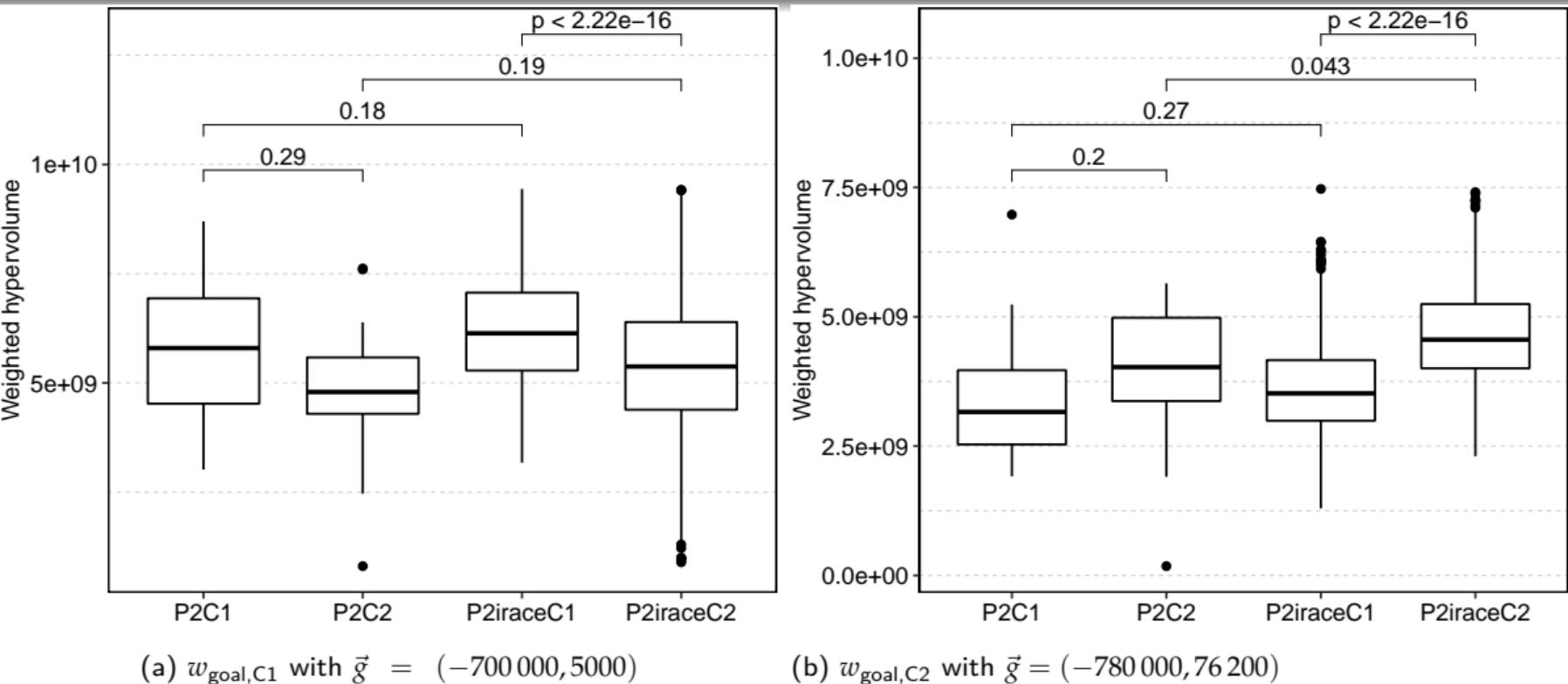
For each unique pair $\{\mathcal{A}, \mathcal{A}'\}$, where \mathcal{A} and \mathcal{A}' are the multiset of approximation fronts produced by two different algorithm configurations

- ① Compute the EAF difference regions in favour of either side $\mathcal{R}_{\mathcal{A}}$ for $\Delta\alpha_{\mathcal{A}, \mathcal{A}'}(\cdot)$ and $\mathcal{R}_{\mathcal{A}'}$ for $-\Delta\alpha_{\mathcal{A}, \mathcal{A}'}(\cdot)$
- ② Compute the total area of each set of regions $\mathcal{R}_{\mathcal{A}}$ and $\mathcal{R}_{\mathcal{A}'}$ by calculating $HV_{\mathcal{R}_{\mathcal{A}}}^w(A^T)$ and $HV_{\mathcal{R}_{\mathcal{A}'}}^w(A^T)$,
where $A^T = \{(f_1^{\min}, f_2^{\min})\}$
- ③ The DM is shown the EAF differences of the pair $\{\mathcal{A}, \mathcal{A}'\}$:

$$\max_{\forall \{\mathcal{A}, \mathcal{A}'\}} \{\min\{HV_{\mathcal{R}_{\mathcal{A}}}^w(A^T), HV_{\mathcal{R}_{\mathcal{A}'}}^w(A^T)\}\}$$

- ④ If the pair selected is not interesting to the DM, or the DM does not feel confident in choosing either side, then the second best pair that satisfies the previous requirement (if such a pair exists) could be shown to the DM.

Boxplots



- The same approximation fronts are evaluated on both subfigures.
- Sets P2C1 and P2C2 contain 16 fronts each, i.e., 16 runs of one configuration of the MOEA.
- Sets P2iraceC1 and P2iraceC2 contain 900 fronts each, i.e., 30 runs of the best configuration of the MOEA returned by the 1st to 30th run of set C1.

- Bi-objective multi-product capacitated production planning problem within a failure-prone batch manufacturing system specialised on cleaning products
- Custom MOEA + discrete event simulator
- MOEA has 4 categorical , 2 real and 2 integer parameters

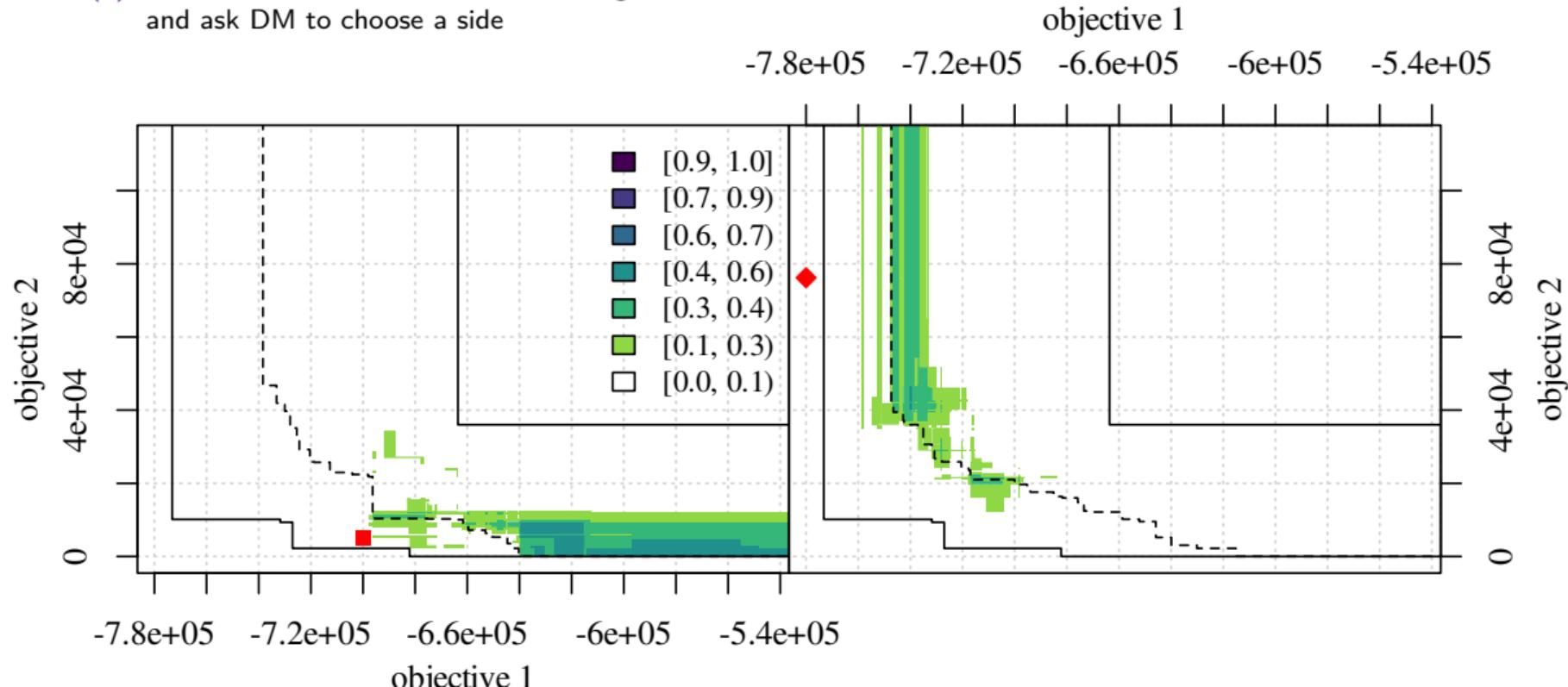
Interactive Tuning Procedure

(1) Run irace guided by *unweighted* HV (budget = 1000 MOEA runs)

(2) Select 2 configurations showing the largest EAF differences

(3) Show EAF differences between 2 configurations

and ask DM to choose a side

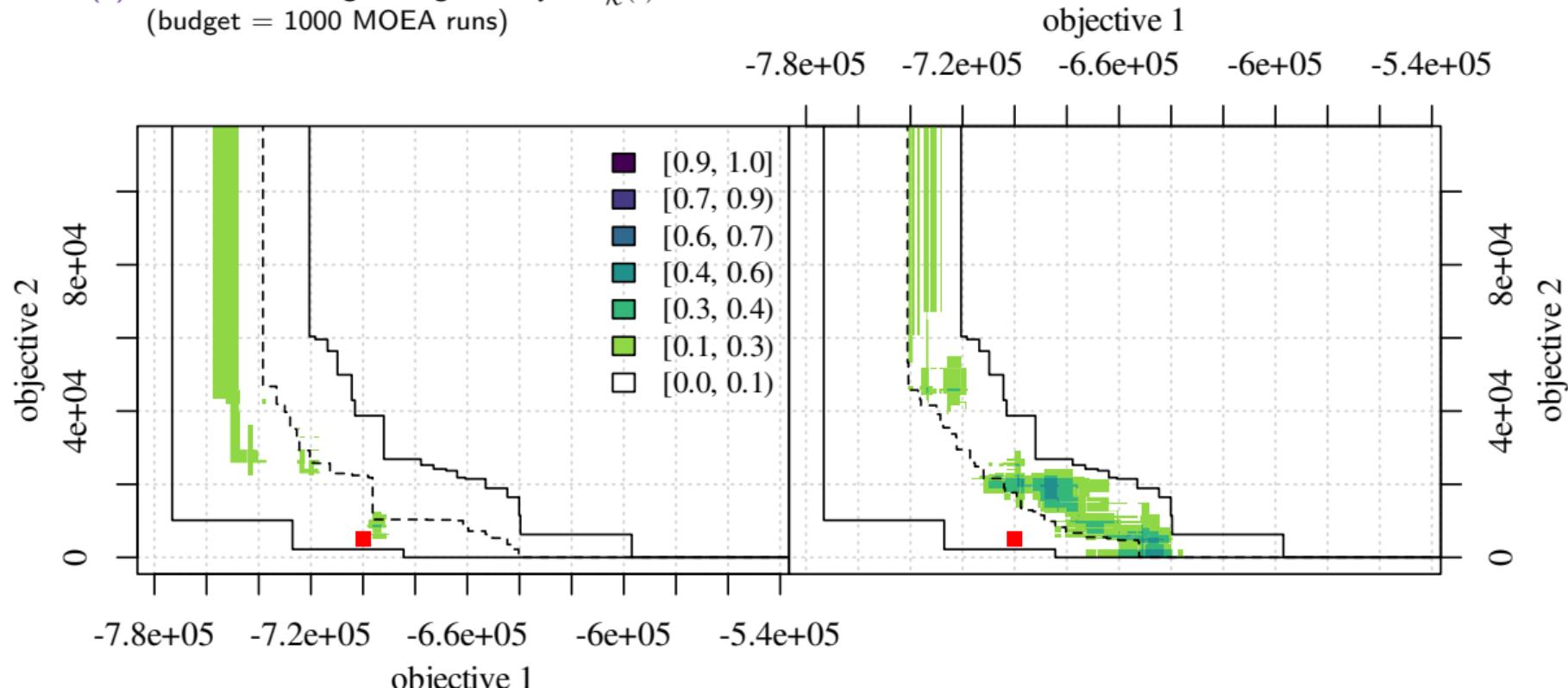


Interactive Tuning Procedure

(4) Compute regions \mathcal{R} in favour of chosen side

(5) Create $HV_{\mathcal{R}}^w(\cdot)$ based on chosen regions

(6) Continue running irace guided by $HV_{\mathcal{R}}^w(\cdot)$
(budget = 1000 MOEA runs)



Interactive Tuning Procedure

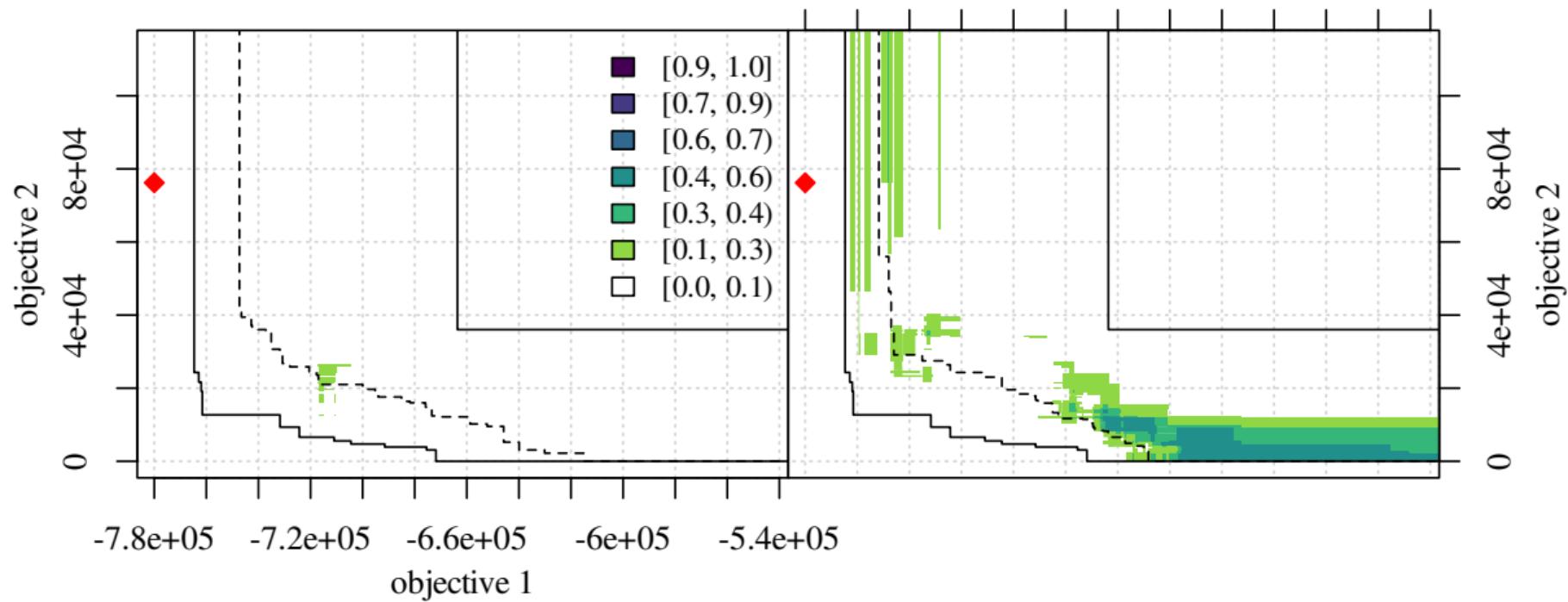
(4) Compute regions \mathcal{R} in favour of chosen side

(5) Create $HV_{\mathcal{R}}^w(\cdot)$ based on chosen regions

(6) Continue running irace guided by $HV_{\mathcal{R}}^w(\cdot)$

objective 1

-7.8e+05 -7.2e+05 -6.6e+05 -6e+05 -5.4e+05



Interactive Tuning Procedure

